

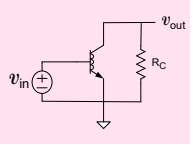
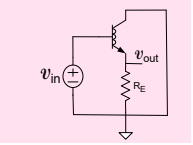
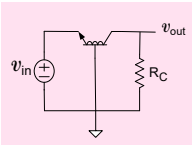
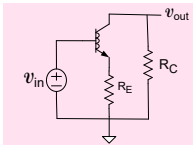
EE 330

Lecture 33

- High Gain Amplifiers
- Current Sources and Mirrors

Review From Previous Lecture


Basic Amplifier Application Gain Table (for low-frequency operation)

	CE/CS		CC/CD		CB/CG		CEwRE/CSwRS	
	BJT	MOS	BJT	MOS	BJT	MOS	BJT	MOS
A_V	 $-g_m R_C$ $-\frac{I_{CQ} R_C}{V_t}$		 $\frac{g_m}{g_m + g_E}$ $\frac{I_{CQ} R_E}{I_{CQ} R_E + V_t}$		 $g_m R_C$ $\frac{I_{CQ} R_C}{V_t}$		 $-\frac{R_C}{R_E}$	
R_{in}	r_{π} $\frac{\beta V_t}{I_{CQ}}$		$r_{\pi} + \beta R_E$ $\frac{\beta V_t}{I_{CQ}} + \beta R_E \approx \beta R_E$		g_m^{-1} $\frac{V_t}{I_{CQ}}$		$r_{\pi} + \beta R_E$ $\beta \left(\frac{V_t}{I_{CQ}} + R_E \right) \approx \beta R_E$	
R_{out}	R_C		g_m^{-1} $\frac{V_t}{I_{CQ}}$		R_C		R_C	

(not two-port models for the four structures)

Can use these equations only when small signal circuit is **EXACTLY** like that shown !!

Basic Amplifier Structures

1. Common Emitter/Common Source
 2. Common Collector/Common Drain
 3. Common Base/Common Gate
 4. Common Emitter with R_E / Common Source with R_S
 5. Cascode (actually CE:CB or CS:CG cascade)
 6. Darlington (special CC:CE or CD:CS cascade)
- 
- Will be discussed later

The first 4 are most popular

High Frequency and Low Frequency Operation

Basic amplifier structures that were just discussed were all assumed to be operating at frequencies where the parasitic capacitances in the devices and circuits do not affect the small-signal operation

- This can be viewed as **low-frequency operation** (including dc)

Major emphasis on amplifiers will be for low-frequency operation in this course

If frequency of small-signal inputs is increased enough, parasitic capacitances in the devices will affect performance. In these cases, lumped models for the devices can include the capacitive effects

- This can be viewed as **high-frequency operation**

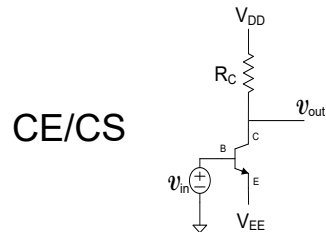
Will spend a little bit of time later discussing high-frequency operation

If frequency of small-signal inputs is increased even more, parasitic capacitances in the devices will affect performance but distributed rather than lumped models of devices and layouts will be required.

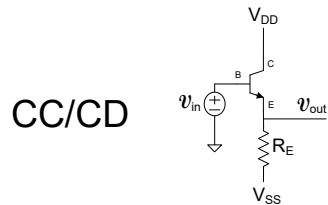
- This can be viewed as **rf operation** (radio frequency)

rf operation will not be discussed in this course

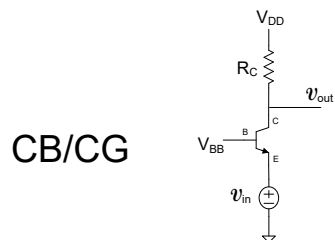
Basic Amplifier Characteristics Summary



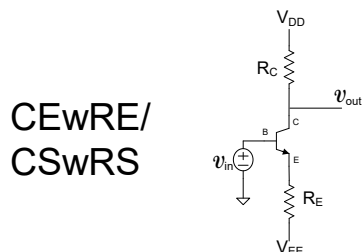
- Large inverting gain
- Moderate input impedance
- Moderate (or high) output impedance
- Widely used as the basic high gain inverting amplifier



- Gain very close to +1 (little less)
- High input impedance for BJT (high for MOS)
- Low output impedance
- Widely used as a buffer

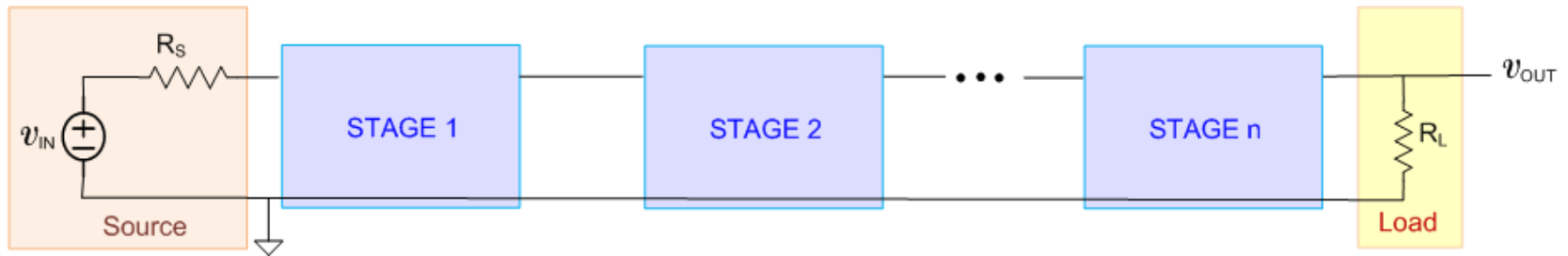


- Large noninverting gain
- Low input impedance
- Moderate (or high) output impedance
- Used more as current amplifier or, in conjunction with CD/CS to form two-stage cascode



- Reasonably accurate but somewhat small gain (resistor ratio)
- High input impedance
- Moderate output impedance
- Used when more accurate gain is required

Cascaded Amplifiers

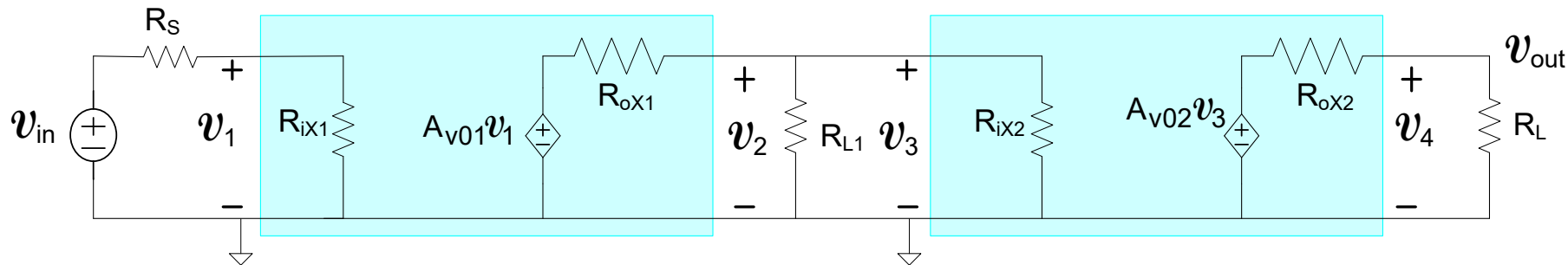


- Amplifier cascading widely used to enhance gain
- Amplifier cascading widely used to enhance other characteristics and/or alter functionality as well
e.g. (R_{IN} , BW, Power, R_O , Linearity, Impedance Conversion..)

Repeat from earlier discussions on amplifiers

Cascaded Amplifier Analysis and Operation

Case 1: All stages Unilateral

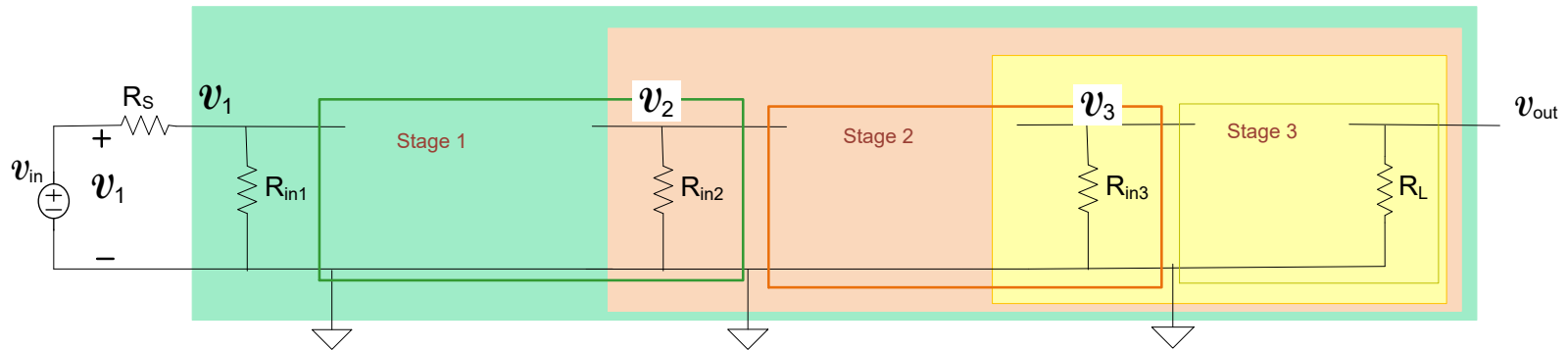


$$A_V = \frac{v_{out}}{v_{in}} = \left(\frac{R_{iX1}}{R_{iX1} + R_s} \right) A_{V01} \left(\frac{R_{L1} // R_{iX2}}{R_{L1} // R_{iX2} + R_{oX1}} \right) A_{V02} \left(\frac{R_L}{R_L + R_{oX2}} \right)$$

Accounts for all loading between stages !

Formalization of cascade circuit analysis working from load to input: (when stages are unilateral or not unilateral)

Case 2: One or more stages may be not unilateral

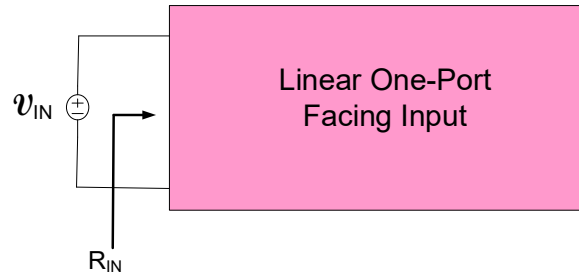


R_{in_k} includes effects of all loading
 Must recalculate if any change in loading
 Analysis systematic and rather simple

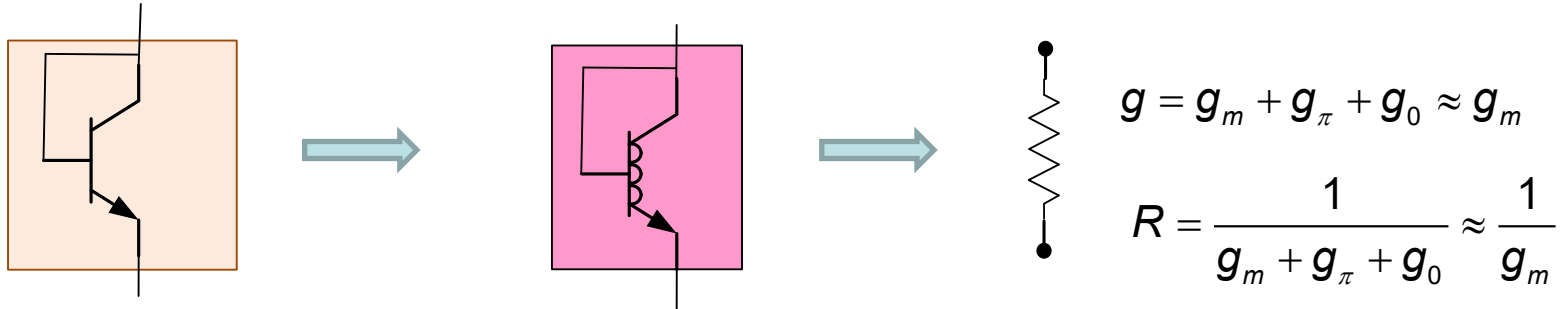
$$\frac{v_{OUT}}{v_{IN}} = \frac{v_1}{v_{IN}} \frac{v_2}{v_1} \frac{v_3}{v_2} \frac{v_{OUT}}{v_3}$$

This was the approach used in analyzing the previous cascaded amplifier

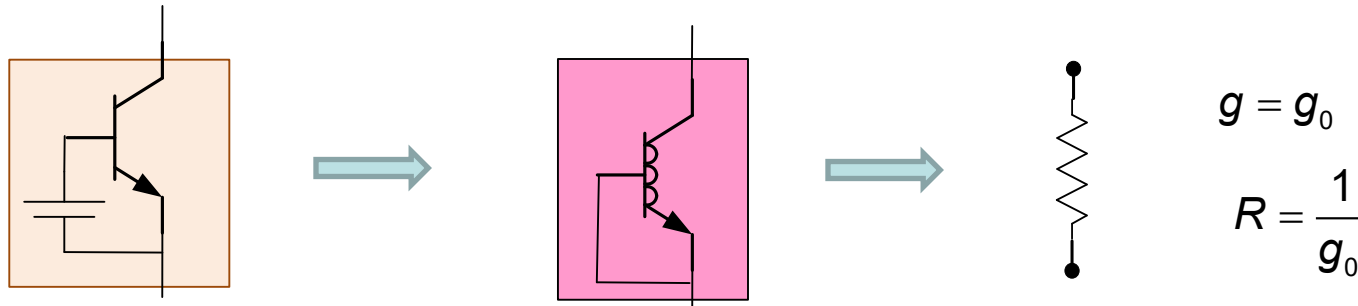
Review: Small-signal equivalent of a one-port



“Diode-connected transistor”

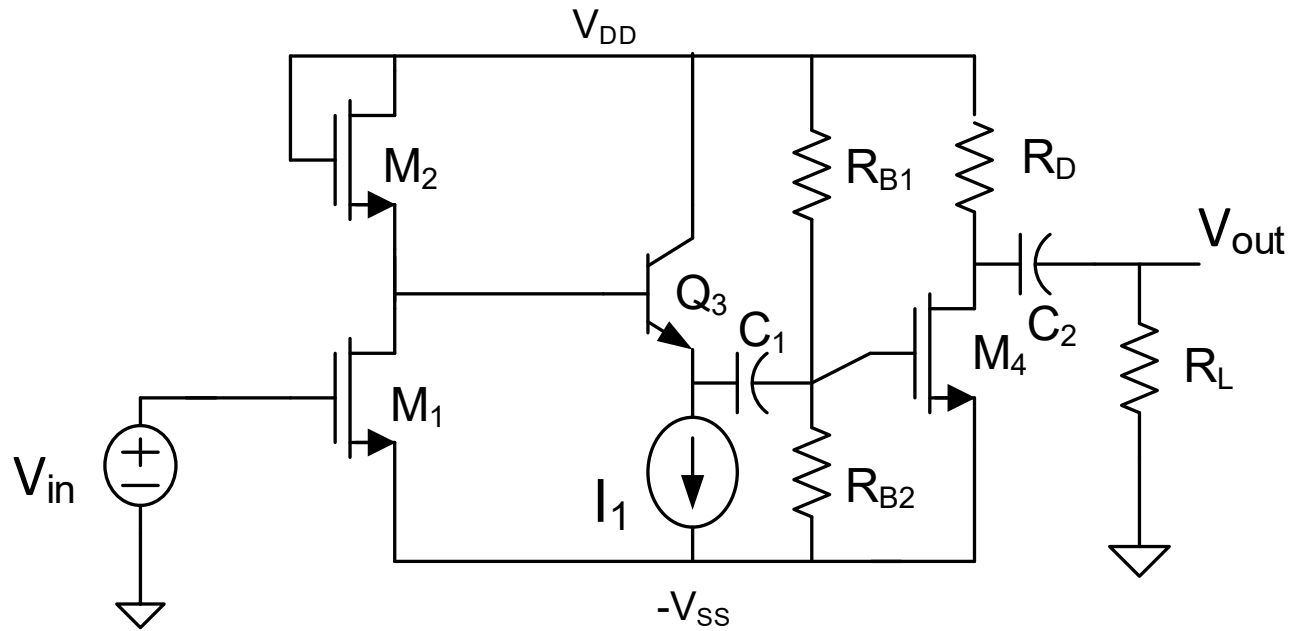


“BE - connected transistor”



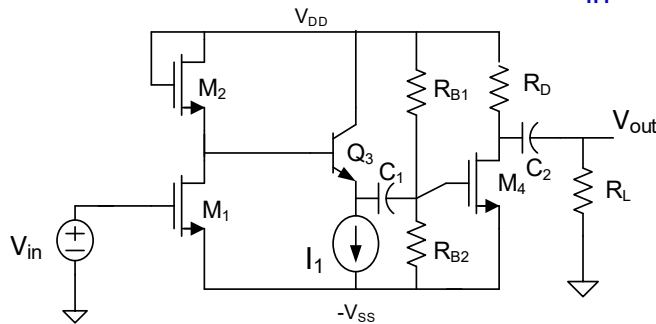
Example 2: $A_v = \frac{v_{out}}{v_{in}} = ?$

Express in terms of small-signal parameters

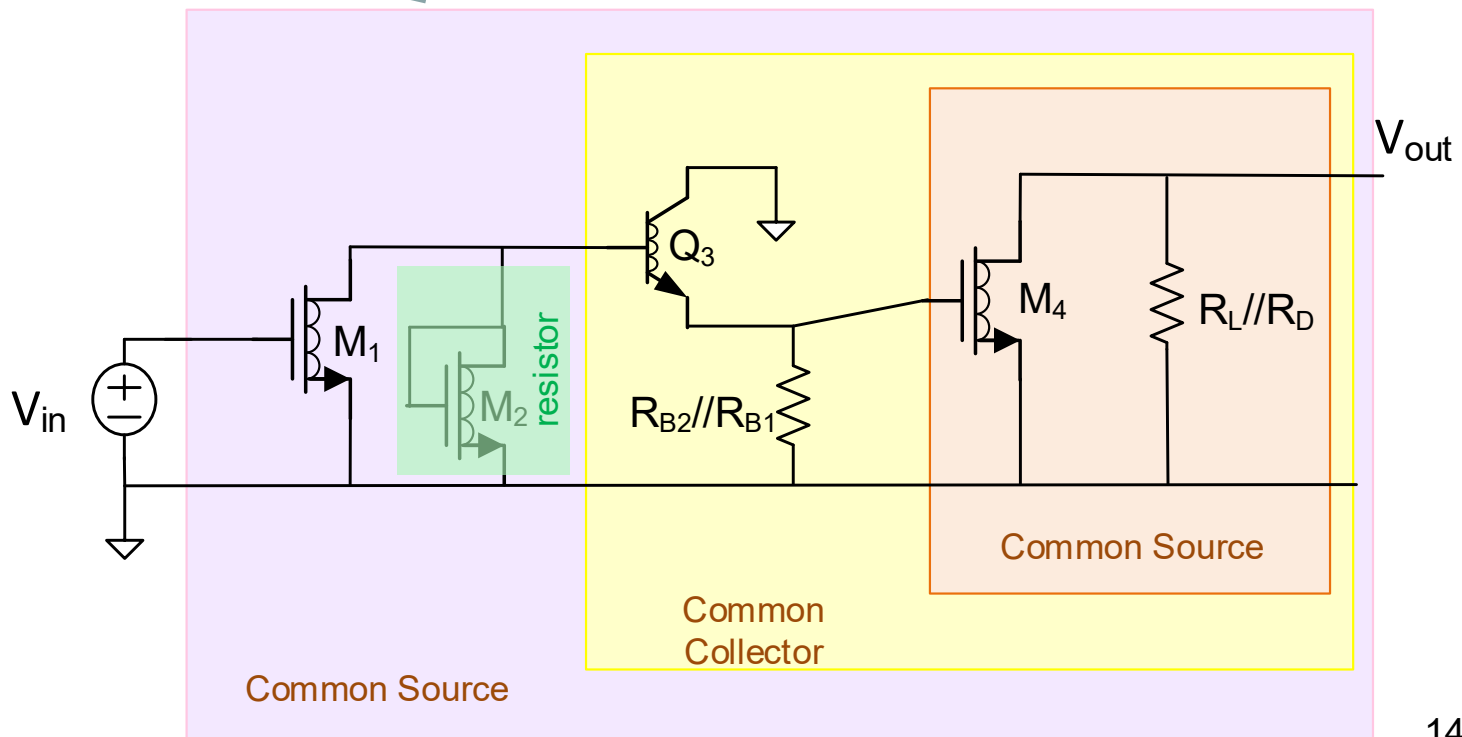


Example 2: $A_v = \frac{v_{out}}{v_{in}} = ?$

Express in terms of small-signal parameters



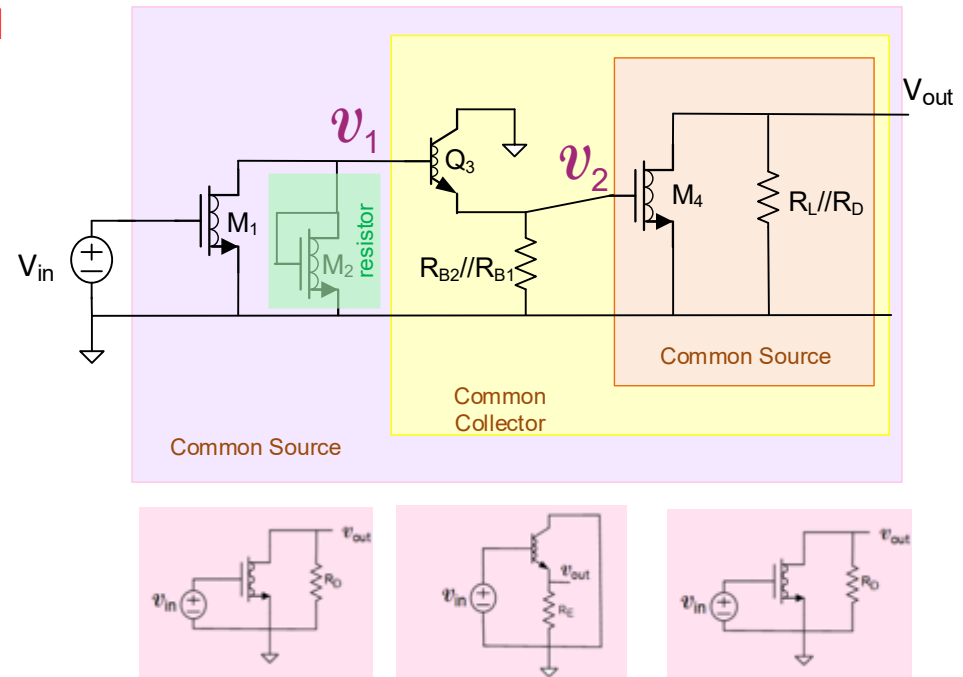
visualize



Example 2: $A_V = \frac{v_{out}}{v_{in}} = ?$

Express in terms of small-signal parameters

Gain Calculation in terms of Small-Signal Parameters



$$\frac{v_{OUT}}{v_2} =$$

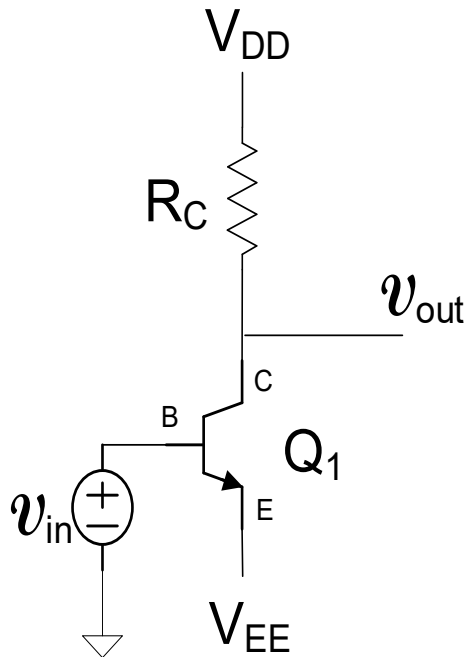
$$\frac{v_2}{v_1} =$$

$$\frac{v_1}{v_{in}} =$$

$$\text{If } r_{\pi} + \beta(R_{B1} // R_{B2}) \gg 1/g_{m2}$$

$$A_V = \frac{v_{out}}{v_2} \frac{v_2}{v_1} \frac{v_1}{v_{in}} \cong \left[-g_{m4} (R_D // R_L) \right] [1] \left[\frac{-g_{m1}}{g_{m2}} \right]$$

High-gain BJT amplifier



$$A_V = \frac{-g_m}{g_0 + G_C} \cong -g_m R_C$$

To make the gain large, it appears that all one needs to do is make R_C large !

$$A_V \cong -g_m R_C = \frac{-I_{CQ} R_C}{V_t}$$

But V_t is fixed at approx 25mV and to keep Q_1 in forward active with large signal swing, $I_{CQ} R_C < (V_{DD} - V_{EE})/2$

$$|A_V| < \frac{V_{DD} - V_{EE}}{2V_t}$$

If $V_{DD} - V_{EE} = 5V$,

$$|A_V| < \frac{5V}{2 \bullet 25mV} = 100$$

- Gain is practically limited with this supply voltage to around 100
- And in extreme case, limited to about 200 with this supply voltage with very small signal swing

High-gain MOS amplifier

$$A_V = \frac{-g_m}{g_0 + G_D} \cong -g_m R_D$$

To make the gain large, it appears that all one needs to do is make R_D large !

$$A_V \cong -g_m R_D = \frac{-2I_{DQ}R_D}{V_{EB}}$$

But V_{EB} is practically limited to around 100mV and for good signal swing, $I_{DQ}R_D < (V_{DD} - V_{SS})/2$

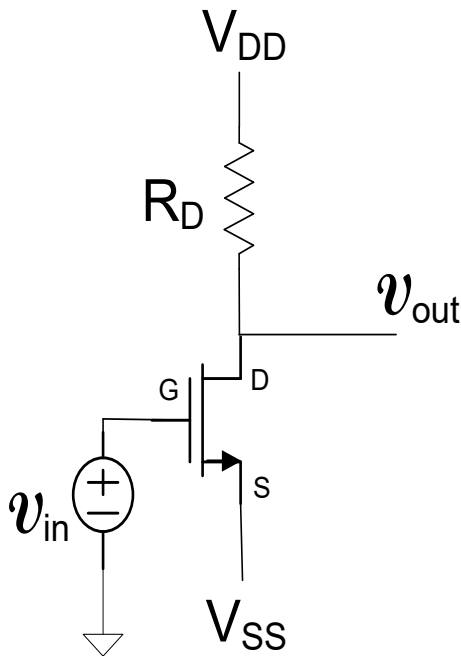
$$|A_V| < \frac{V_{DD} - V_{SS}}{V_{EB}}$$

If $V_{DD} - V_{SS} = 5V$ and $V_{EB} = 100mV$,

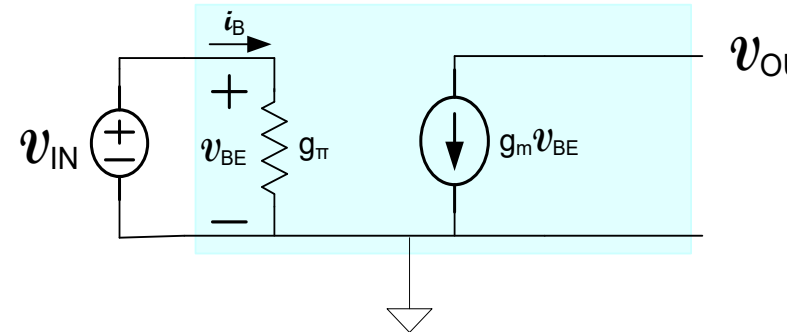
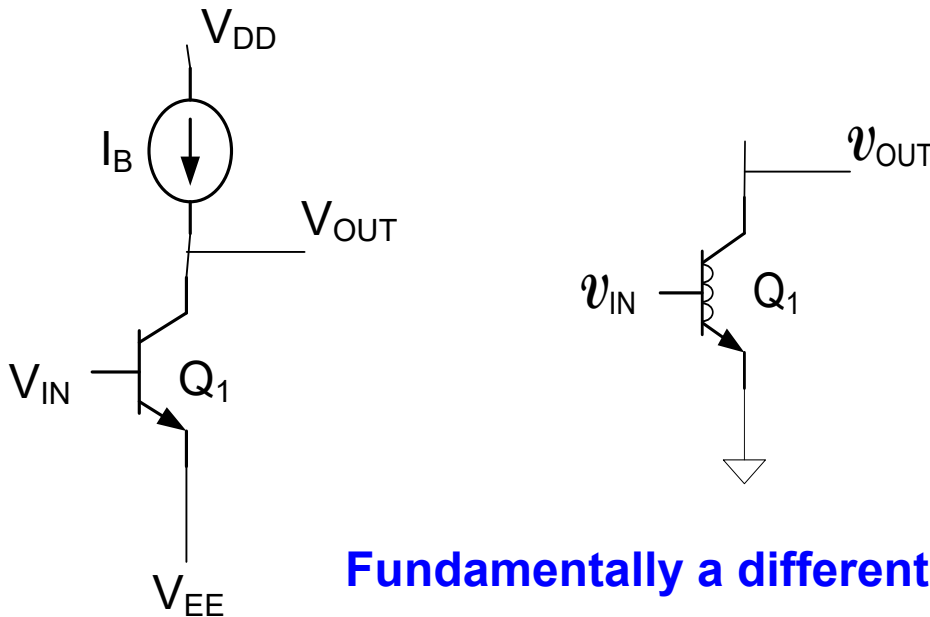
$$|A_V| < \frac{5V}{100mV} = 50$$

Gain is practically limited with this supply voltage to around 50

Are these fundamental limits on the gain of the BJT and MOS Amplifiers?



High-gain amplifier



$$A_V = \frac{-g_m}{0} = -\infty$$

Fundamentally a different circuit

Current source is biasing Q_1

This gain is very large !

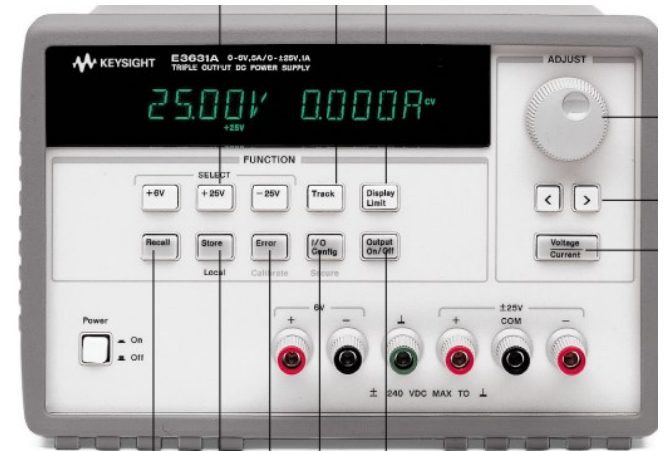
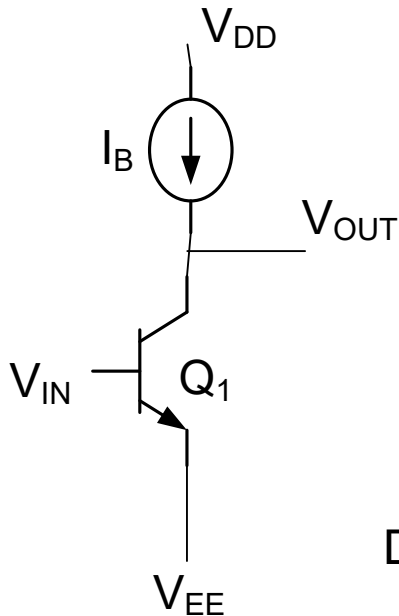
Too good to be true !

Need better model of BJT and MOS device (but we already have it) !

But are current sources really available?



Current Source ???



Voltage Source

Model: 3631A

\$3100??

Did you discuss current sources in EE 201?

Did you have any current sources in the EE 201 laboratory?

Did you have any current sources in the EE 230 laboratory?

Do current sources really exist?

Each of the three Keysight E3631A power supply outputs can operate in either constant-voltage (CV) mode or constant-current (CC) mode. Under certain fault conditions, the power supply cannot operate in either CV or CC mode and becomes unregulated.

Little information about transient response due to changing loads in either voltage mode or current mode

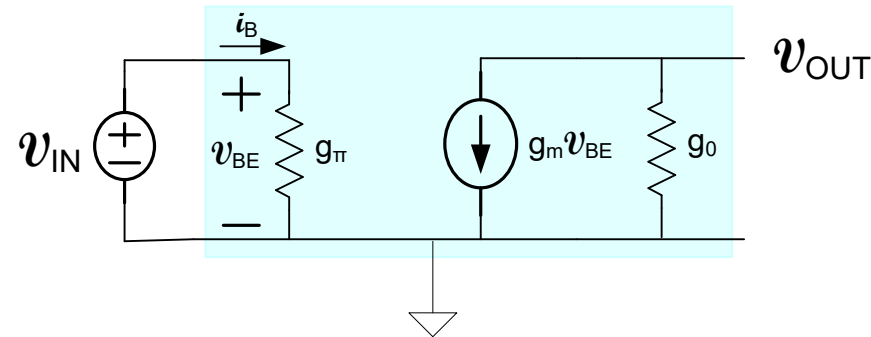
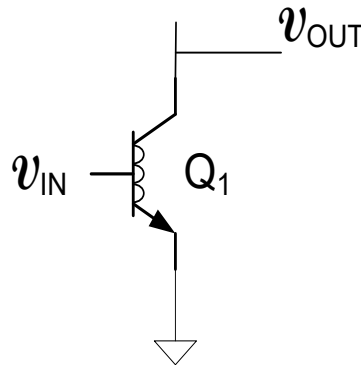
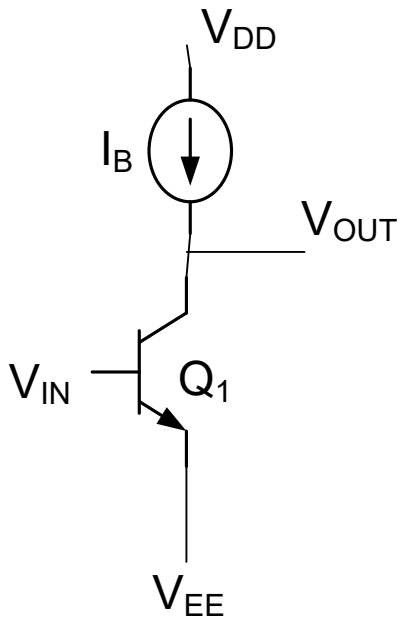
Output ratings (@ 0 °C - 40 °C)			
+6V Output	0 to +6 V ; 0 to 5 A		
+25V Output	0 to +25 V ; 0 to 1 A		
-25V Output	0 to -25 V ; 0 to 1 A		

Stability, \pm (% of output + offset)			
Following a 30-minute warm-up, with the output in the ON state according to the operating mode (CC with load or CV), and with a change in the output over 8 hours under constant load, line, and ambient temperature			
	+6V output	+25V output	-25V output
Voltage	0.03% + 1 mV	0.02% + 2 mV	0.02% + 2 mV
Current	0.1% + 3 mA	0.05% + 1 mA	0.05% + 1 mA

Ripple and noise (with outputs ungrounded, or with either output terminal grounded, 20 Hz to 20 MHz)			
	+6V output	+25V output	-25V output
Voltage	<0.35 mV rms	<0.35 mV rms	<0.35 mV rms
	<2 mV p-p	<2 mV p-p	<2 mV p-p
Current	<2 mA rms	<500 μ A rms	<500 μ A rms

Programming accuracy ^[1] 12 months (@ 25 °C \pm 5 °C), \pm (% of output + offset)			
	+6V output	+25V output	-25V output
Voltage	0.1% + 5 mV	0.05% + 20 mV	0.05% + 20 mV
Current	0.2% + 10 mA	0.15% + 4 mA	0.15% + 4 mA

High-gain amplifier



$$A_V = \frac{-g_m}{g_o}$$

$$A_V = \frac{-I_{CQ}}{V_t I_{CQ}/V_{AF}} = -\frac{V_{AF}}{V_t}$$

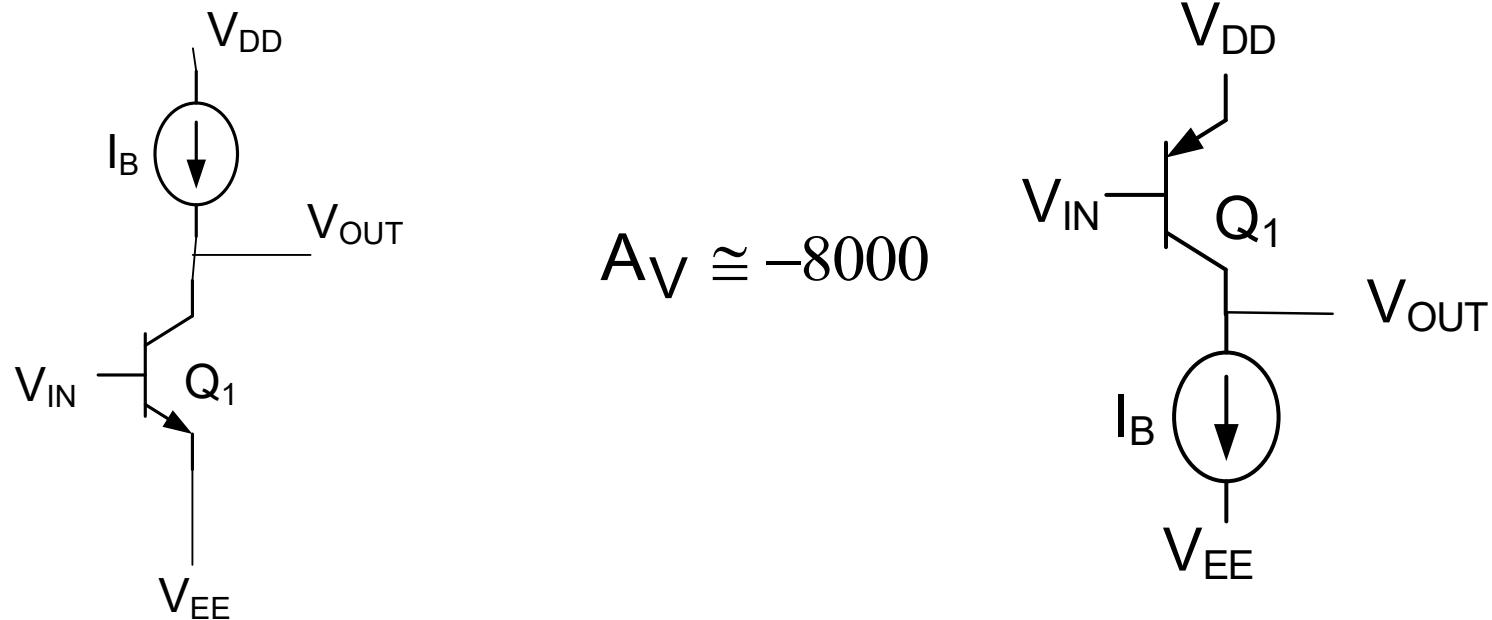
$$A_V = -\frac{V_{AF}}{V_t} \cong \frac{200V}{25mV} = -8000$$

This gain is very large (but realistic) !

And no design parameters affect the gain

But how can we make a current source?

High-gain amplifier

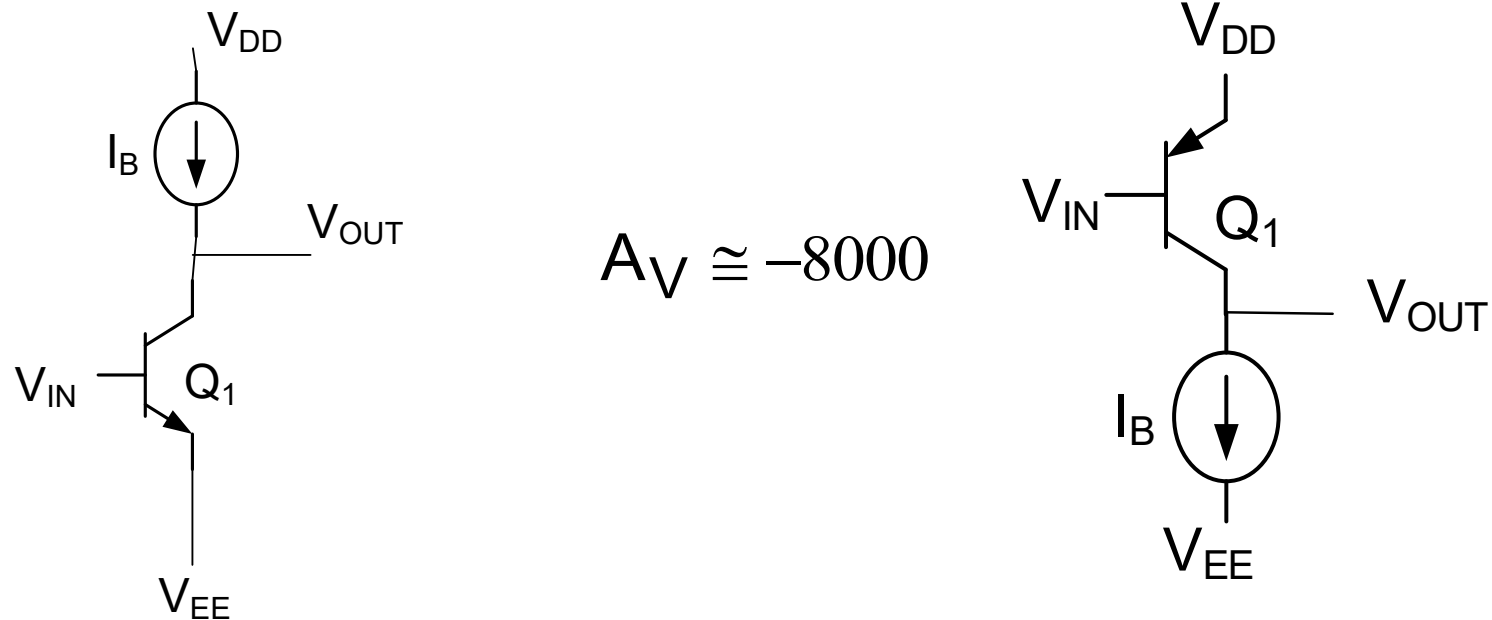


Same gain with both npn and pnp transistors

How can we build the ideal current source?

What is the small-signal model of an actual current source?

High-gain amplifier

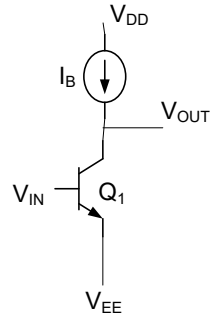
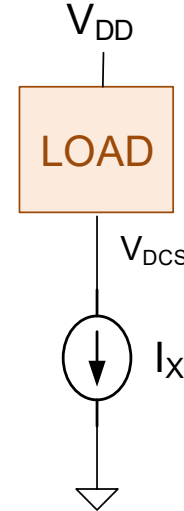
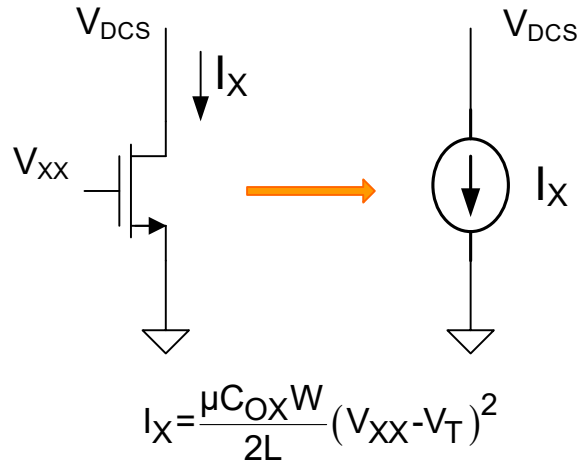


Same gain with both npn and pnp transistors

Will now focus on creating current sources and then return to using these current sources to build high gain amplifiers.

Simple Current Sources

a “sinking” current source



Since I_X is independent of V_{DCS} , acts as an ideal current source (with this model)

Termed a “sinking” current source since current is pulled out of the load

If V_{XX} is available, each dc current source requires only one additional transistor !

Have several methods for generating V_{XX} from V_{DD} (see HW problems)

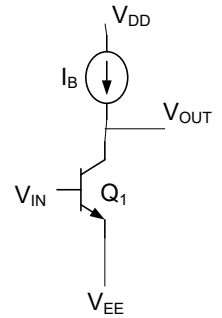
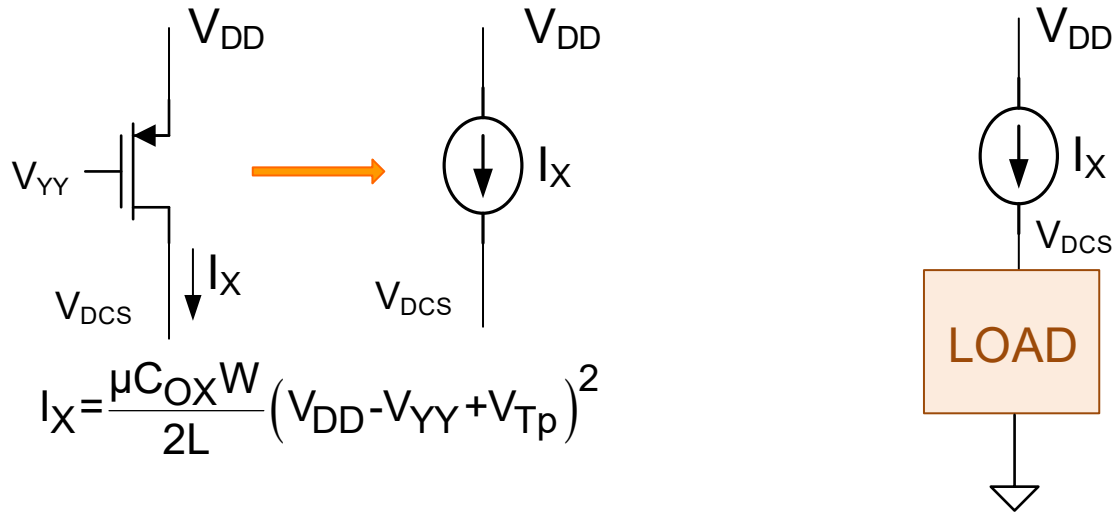
But how good is this current “sink”?

And may not have both MOS and Bipolar devices in most processes!

But for the npn high-gain amplifier considered need a sourcing current

Simple Current Sources

a “sourcing” current source



Since I_X is independent of V_{DCS} , acts as an ideal current source (with this model)

Termed a “sourcing” current source since pushed into the load

If V_{YY} is available, each dc current source requires only one additional transistor !

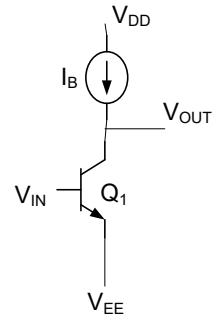
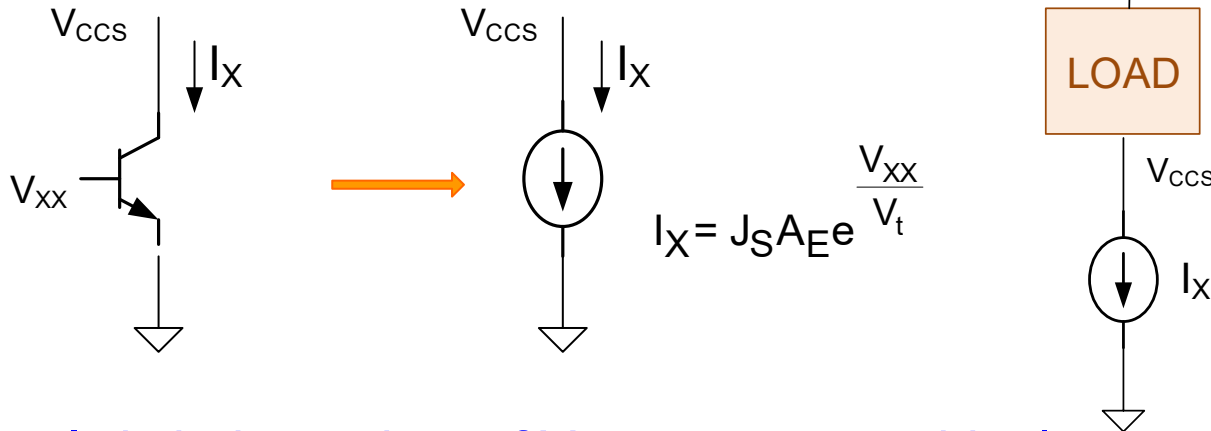
Have several methods for generating V_{YY} from V_{DD} (see HW problems)

But how good is this current “source”?

And may not have both MOS and Bipolar devices in most processes!

Simple Current Sources

a “sinking” current source



Since I_X is independent of V_{CCS} , acts as an ideal current source (with this model)

Termed a “sinking” current source since current is pulled out of the load

If V_{XX} is available, each dc current source requires only one additional transistor !

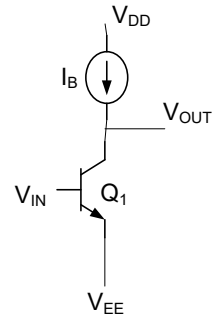
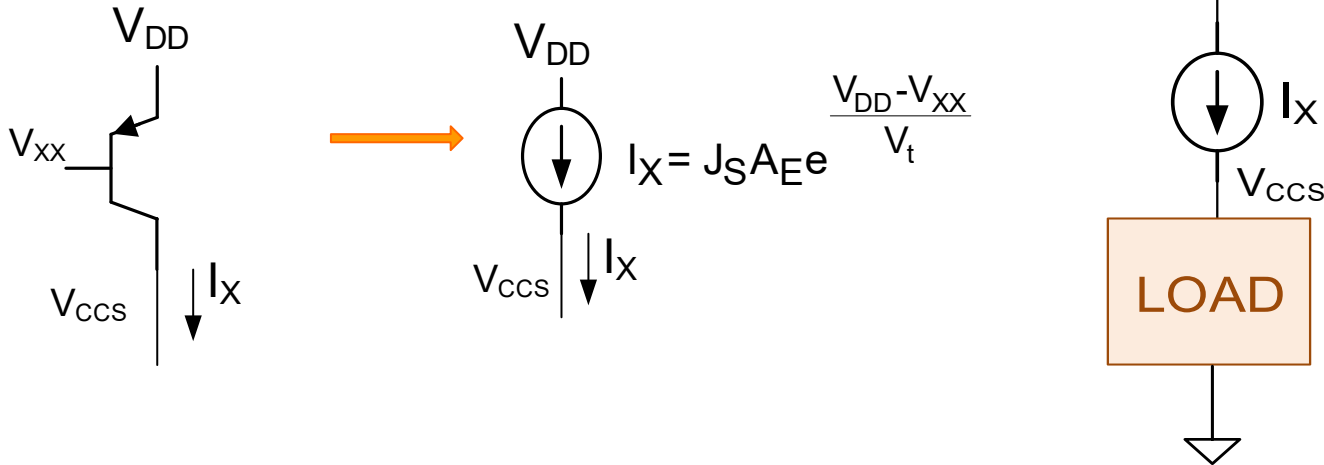
Have several methods for generating V_{XX} from V_{DD} (see HW problems)

But for the npn high-gain amplifier considered need a sourcing current

But how good is this current “sink”?

Simple Current Sources

a “sourcing” current source



Since I_X is independent of V_{CCS} , acts as an ideal current source (with this model)

Termed a “sourcing” current source since pushed into the load

If V_{XX} is available, each dc current source requires only one additional transistor !

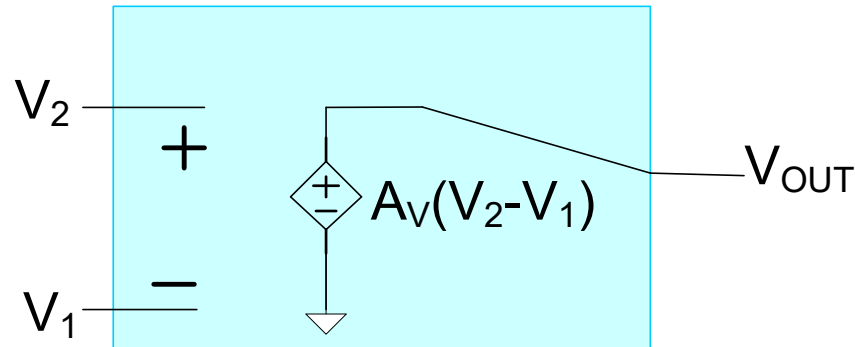
Current highly sensitive to V_{XX} if generated with dc voltage source

Have several methods for generating V_{XX} from V_{DD} (see HW problems)

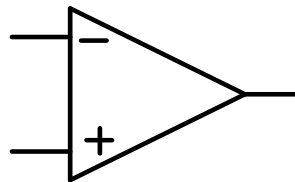
But how good is this current “source”?

Before addressing the issue of how a current source is designed, will consider another circuit that uses current source biasing

The Basic Differential Amplifier

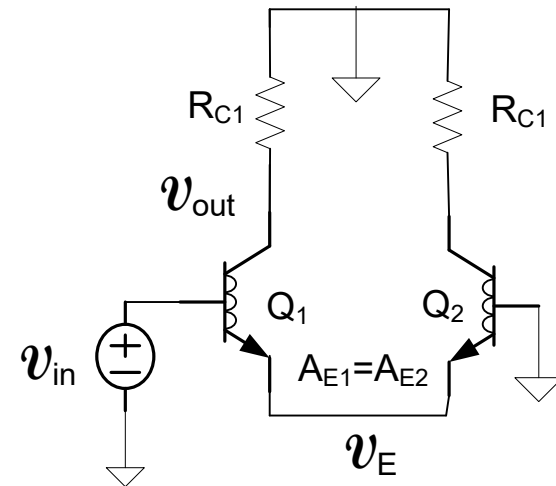
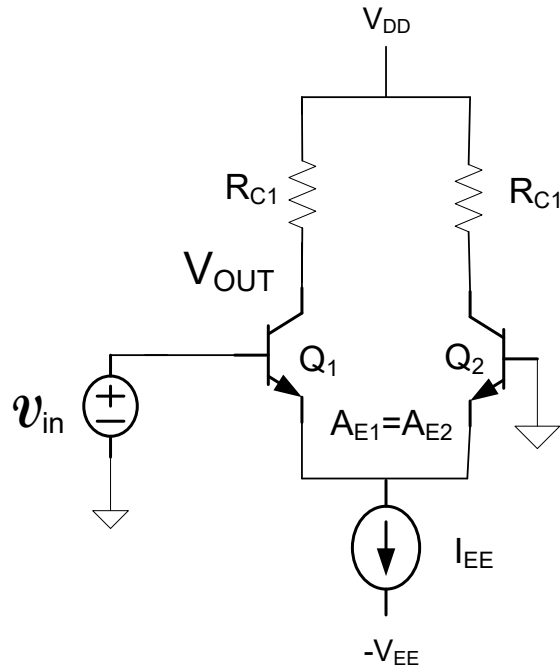


If A_V is large



Operational Amplifier (Op Amp)

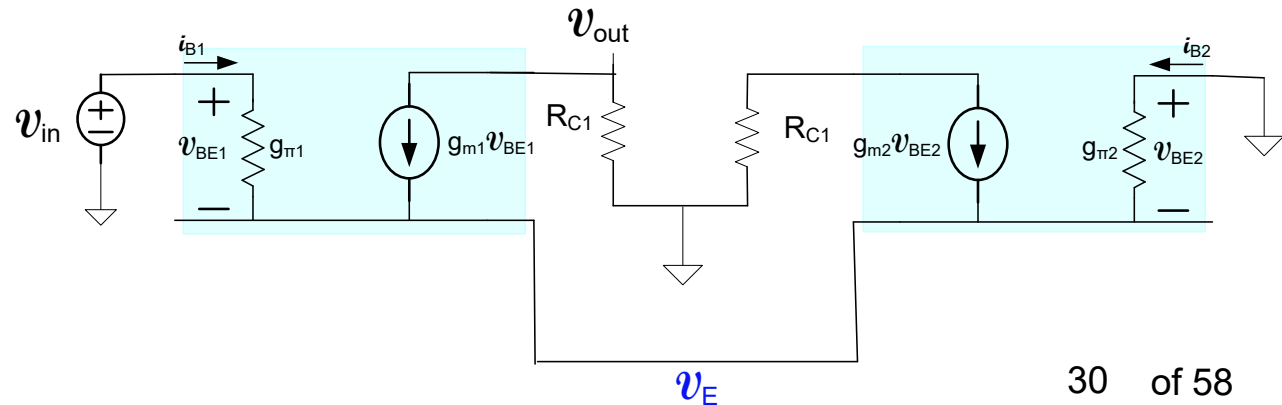
Example: Determine the voltage gain of the following circuit



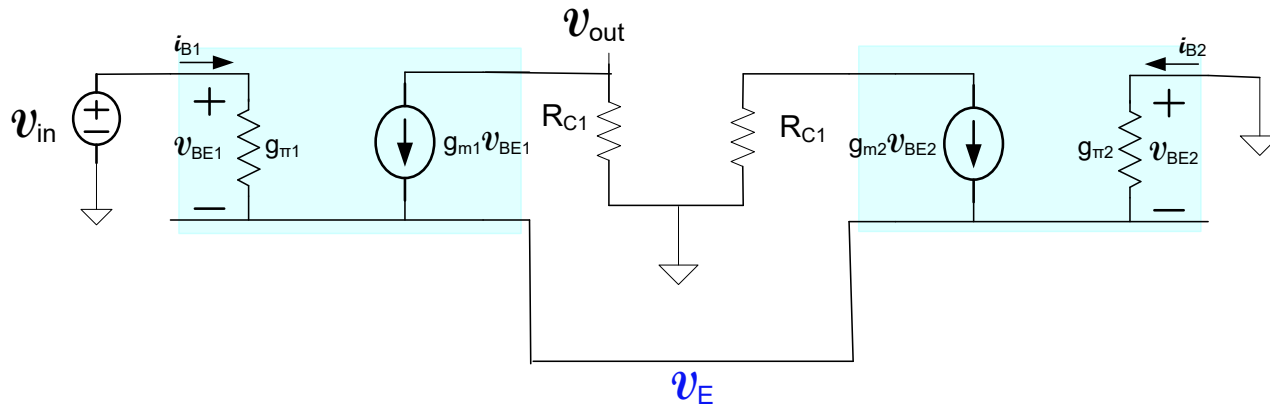
Since symmetric when $v_{IN}=0$

$$I_{C1Q} = I_{C2Q} = \frac{I_{EE}}{2}$$

$$g_{m1} = g_{m2} = \frac{I_{EE}}{2V_t}$$



Example: Determine the voltage gain of the following circuit



$$\left. \begin{aligned} v_E (g_{\pi 1} + g_{\pi 2}) &= g_{\pi 1} v_{IN} + g_{m1} (v_{IN} - v_E) + g_{m2} (-v_E) \\ v_{OUT} &= -R_{C1} g_{m1} (v_{IN} - v_E) \end{aligned} \right\}$$

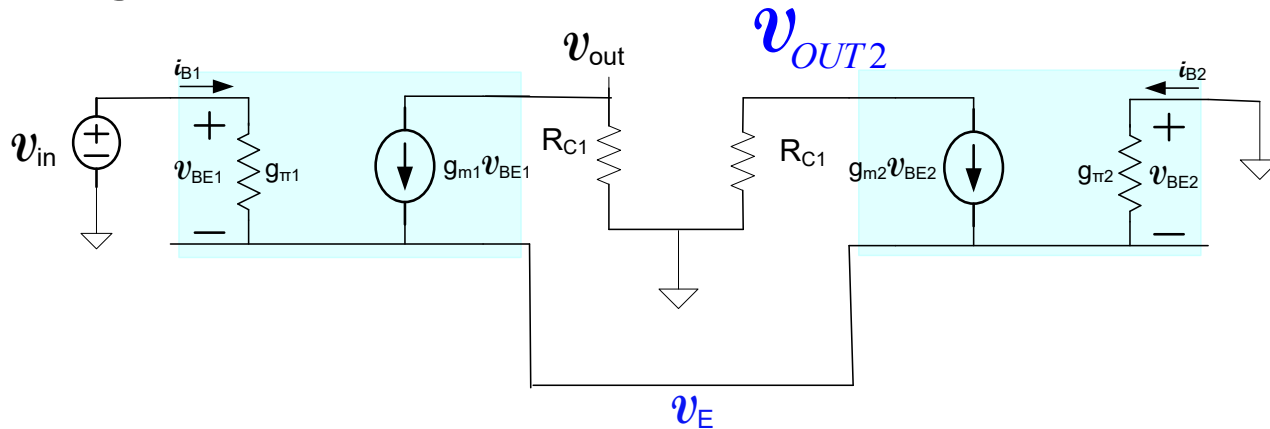
$$v_E (g_{\pi 1} + g_{\pi 2} + g_{m1} + g_{m2}) = v_{IN} (g_{m1} + g_{\pi 1})$$

$$v_E = \frac{(g_{m1} + g_{\pi 1})}{(g_{\pi 1} + g_{\pi 2} + g_{m1} + g_{m2})} v_{IN}$$

$$v_{OUT} = -R_{C1} g_{m1} v_{IN} \left[1 - \frac{(g_{m1} + g_{\pi 1})}{(g_{\pi 1} + g_{\pi 2} + g_{m1} + g_{m2})} \right]$$

$$v_{OUT} = -R_{C1} g_{m1} v_{IN} \left[\frac{g_{\pi 1} + g_{\pi 2} + g_{m1} + g_{m2} - (g_{m1} + g_{\pi 1})}{(g_{\pi 1} + g_{\pi 2} + g_{m1} + g_{m2})} \right]$$

Example: Determine the voltage gain of the following circuit



$$v_{OUT} = -R_{C1}g_{m1}v_{IN} \left[\frac{g_{\pi1} + g_{\pi2} + g_{m1} + g_{m2} - (g_{m1} + g_{\pi1})}{(g_{\pi1} + g_{\pi2} + g_{m1} + g_{m2})} \right]$$

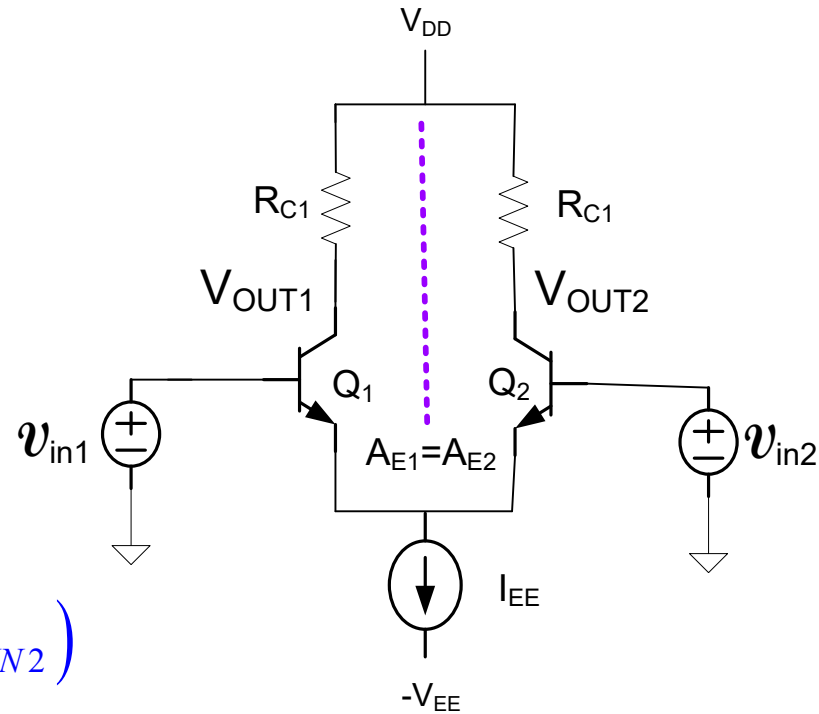
$$v_{OUT} \cong -R_{C1}g_{m1}v_{IN} \left[\frac{g_{m2}}{(g_{m1} + g_{m2})} \right]$$

$$v_{OUT} \cong \left[\frac{-R_{C1}g_{m1}}{2} \right] v_{IN}$$

Can also be shown that

$$v_{OUT2} \cong \left[\frac{R_{C1}g_{m1}}{2} \right] v_{IN}$$

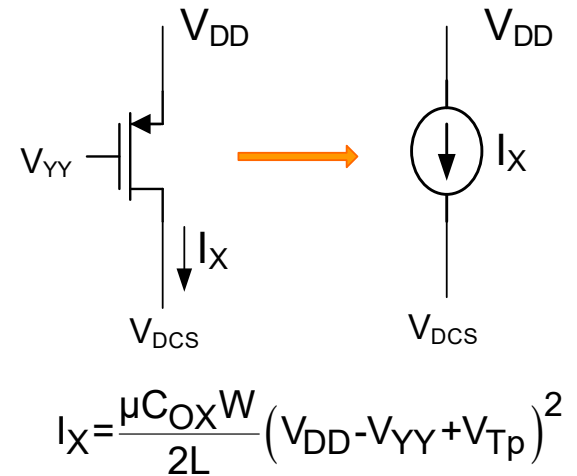
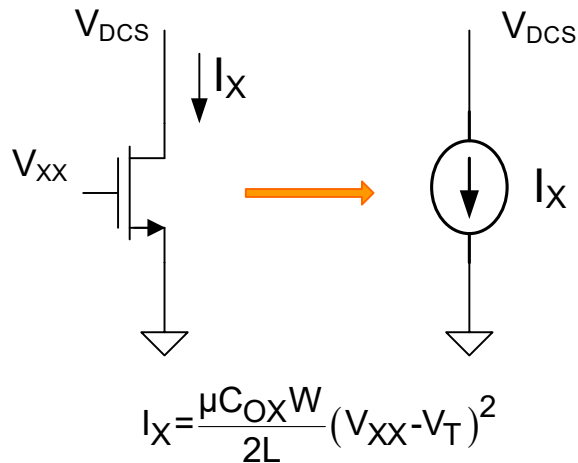
Differential amplifier



$$v_{OUT1} \cong -\left[\frac{R_{C1}g_{m1}}{2}\right](v_{IN1} - v_{IN2})$$
$$v_{OUT2} \cong \left[\frac{R_{C1}g_{m1}}{2}\right](v_{IN1} - v_{IN2})$$

- Very useful circuit
- This is a basic Op Amp
- Uses a current source and V_{DD} for biasing (no biasing resistors or caps!)
- But – needs a dc current source !!!!

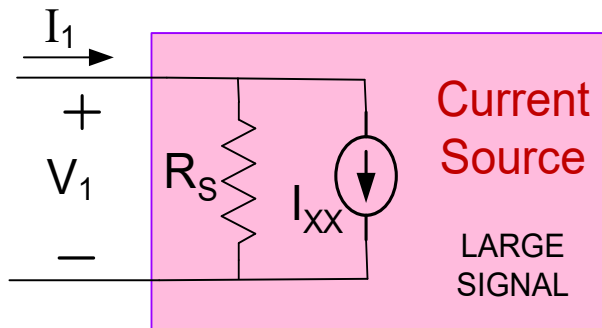
Simple Current Sources



But how good are these current sources?

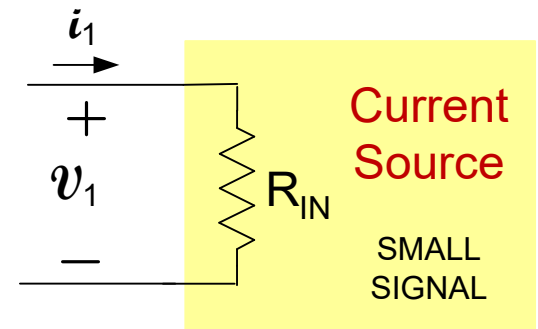
Model of dc Current Source

“Reasonable dc Current Source”



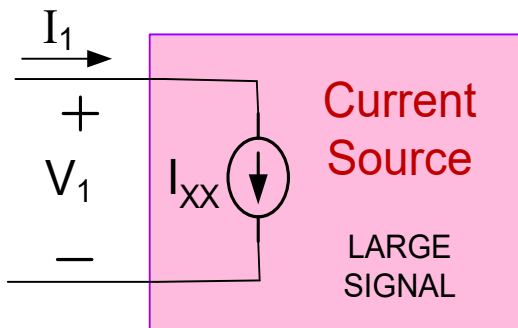
I_{XX} independent of V_1 and t , R_S large

Small-signal model of dc current source (since one-port)

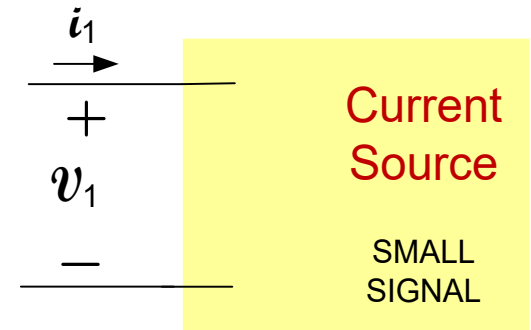


want R_{IN} large

Ideal dc Current Source



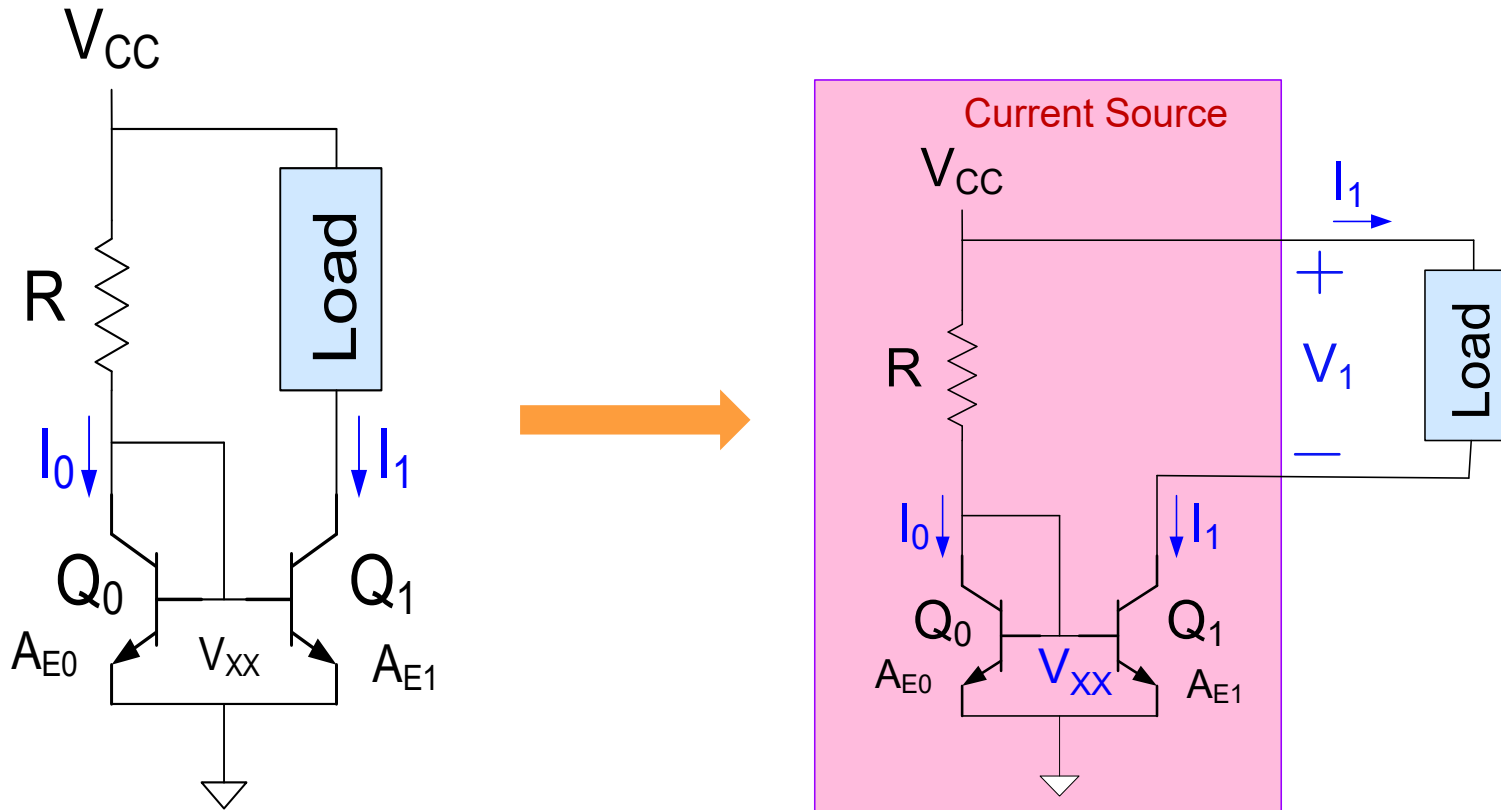
I_{XX} independent of V_1 and t



$R_{IN} = \infty$ 36 of 58

Current Sources/Mirrors

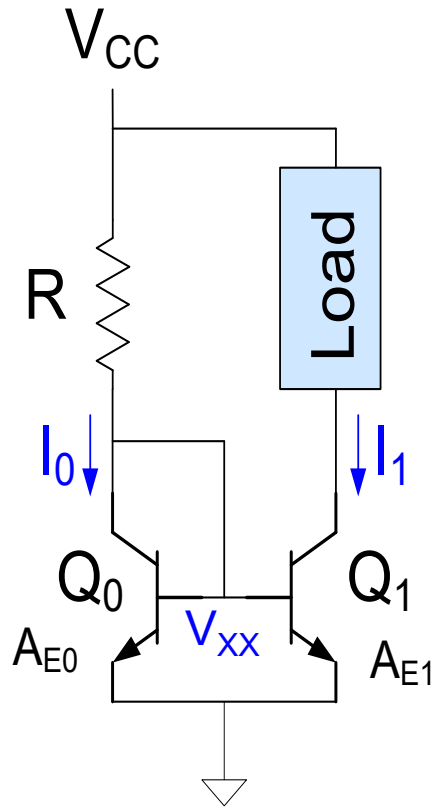
Will show circuit in red behaves as a current source



R and Q_0 simply generate voltage V_{XX} in previous circuit

But sensitivity of I_1 is much smaller than using voltage source for generating V_{XX}

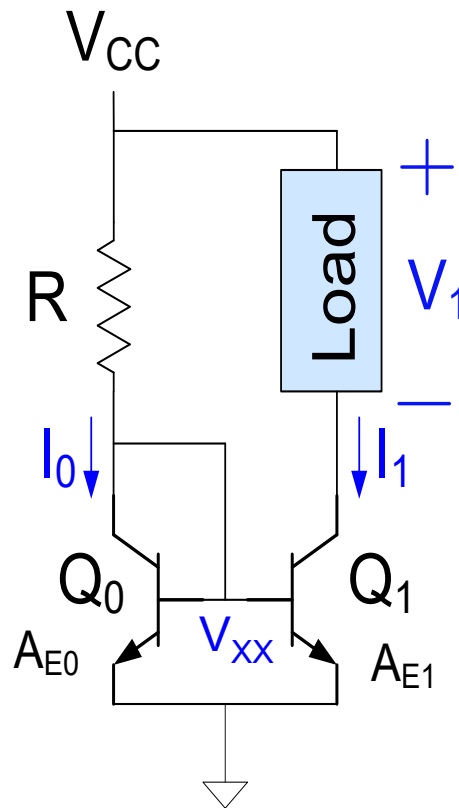
Current Sources/Mirrors



$$I_0 \cong \frac{(V_{CC} - 0.6V)}{R}$$

If the base currents are neglected

Current Sources/Mirrors



$$I_0 \cong \frac{(V_{CC} - 0.6V)}{R}$$

If the base currents are neglected

$$\left. \begin{aligned} I_0 &= J_S A_{E0} e^{\frac{V_{BE0}}{V_t}} \\ I_1 &= J_S A_{E1} e^{\frac{V_{BE1}}{V_t}} \end{aligned} \right\}$$

since $V_{BE1} = V_{BE2}$

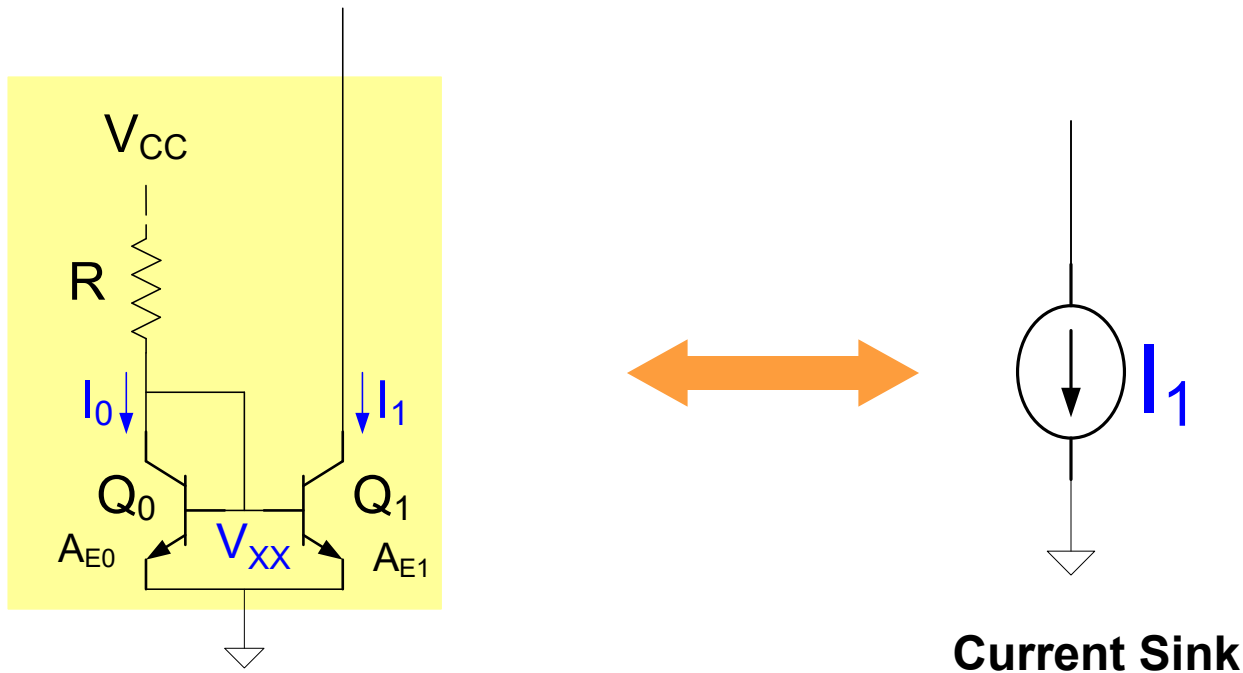
$$I_1 \cong \left(\frac{A_{E1}}{A_{E0}} \right) I_0 = \left(\frac{A_{E1}}{A_{E0}} \right) \frac{V_{CC} - 0.6V}{R}$$

Note I_1 is not a function of V_1

Behaves as a current sink ! So is ideal with this model !!

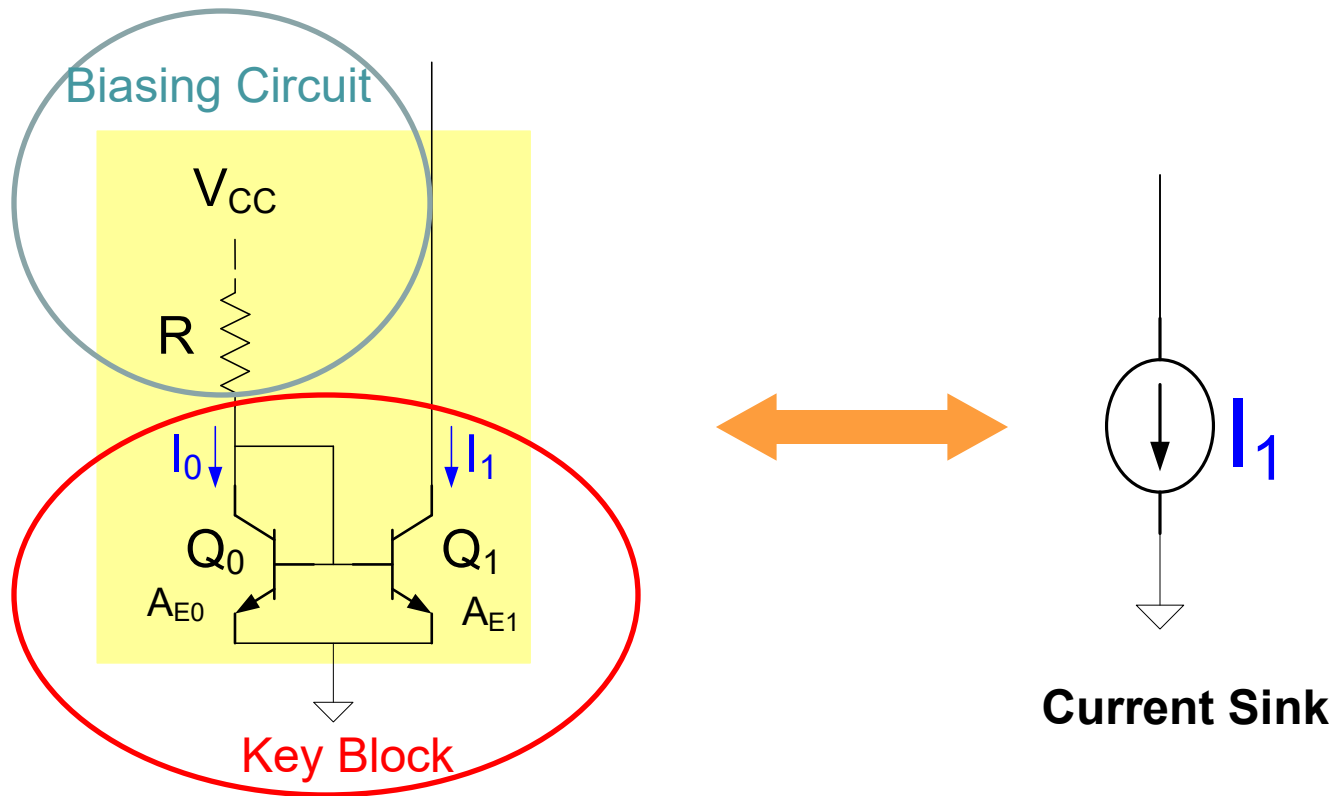
And does not require an additional dc voltage source !!!

Current Sources/Mirrors



- **Multiple Outputs Possible**
- **Can be built for sourcing or sinking currents**
- **Also useful as a current amplifier**
- **MOS counterparts work very well and are not plagued by base current**

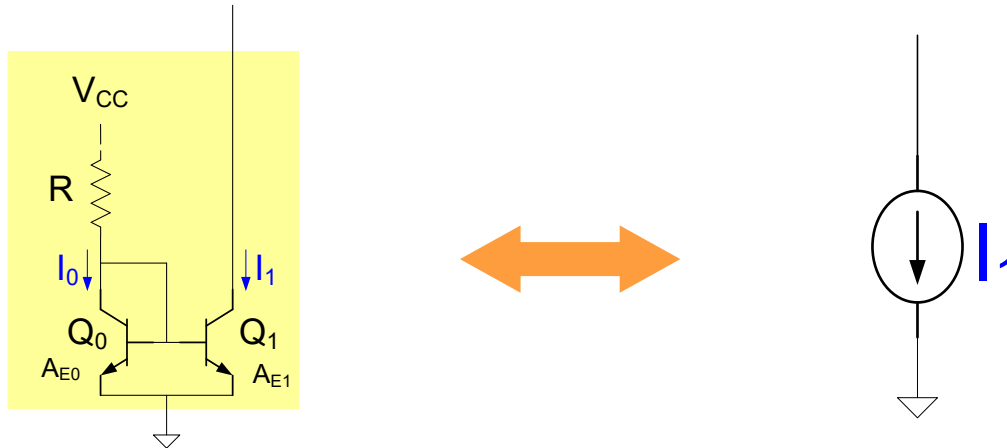
Current Sources/Mirrors



Two ways to look at this circuit:

- Q_0 and R bias Q_1
- R biases the $Q_0 : Q_1$ block

Current Sources/Mirrors



Current Sources are Seldom Available in Basic Laboratories:

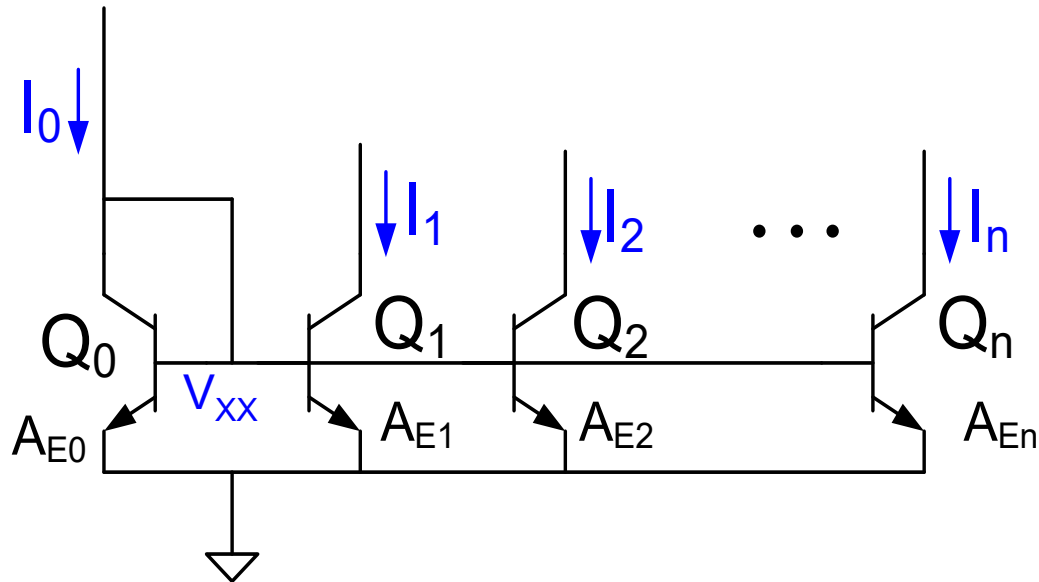
Biasing of board-level and discrete electronic circuits is usually done with voltage sources, resistors, and capacitors

Biasing resistors and capacitors are used very sparingly in MOS circuits

Will show on-chip current sources can be very small

Biasing of on-chip circuits is often done with current sources instead of R's and C's

Current Sources/Mirrors

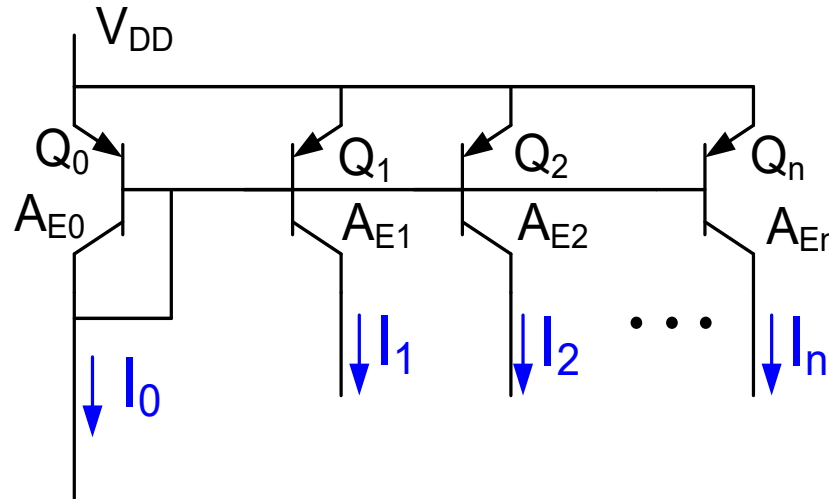


Multiple-Output Bipolar Current Sink

If the base currents are neglected

$$I_k = \left[\frac{A_{Ek}}{A_{E0}} \right] I_0$$

Current Sources/Mirrors

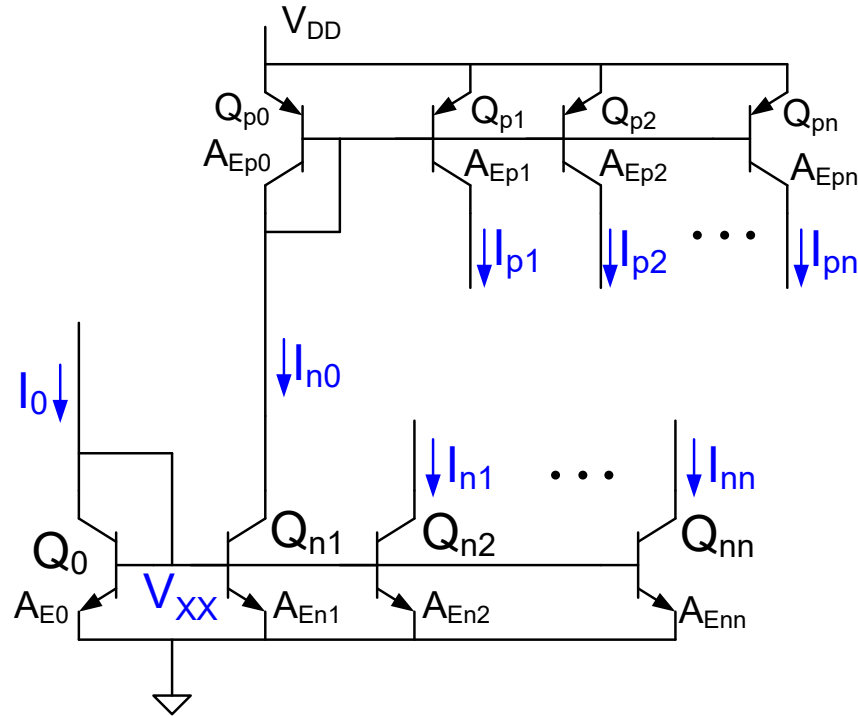


Multiple-Output Bipolar Current Source

If the base currents are neglected

$$I_k = \left[\frac{A_{Ek}}{A_{E0}} \right] I_0$$

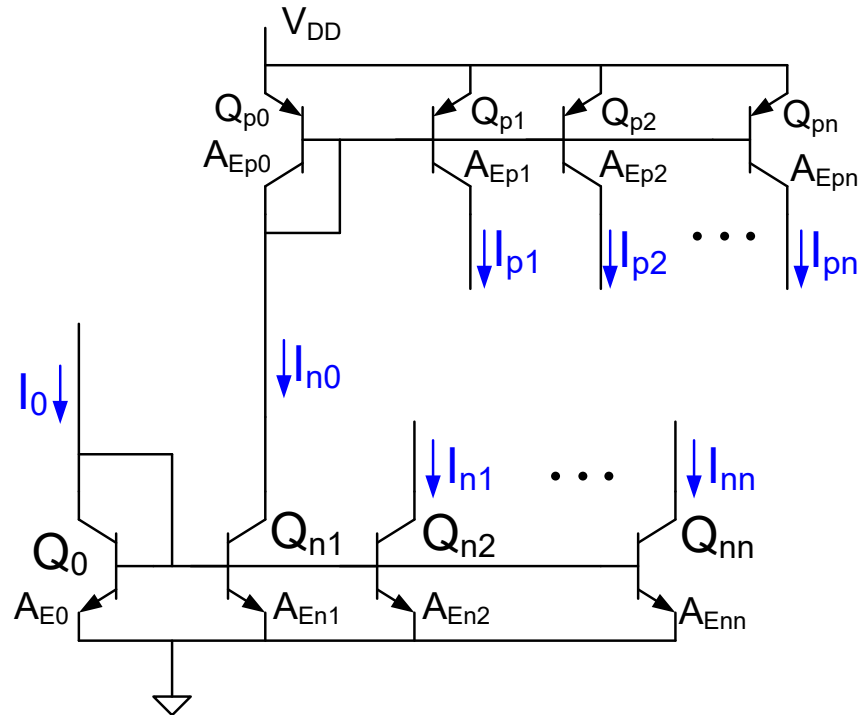
Current Sources/Mirrors



Multiple-Output Bipolar Current Source and Sink

$$I_{nk} = ? \quad I_{pk} = ?$$

Current Sources/Mirrors

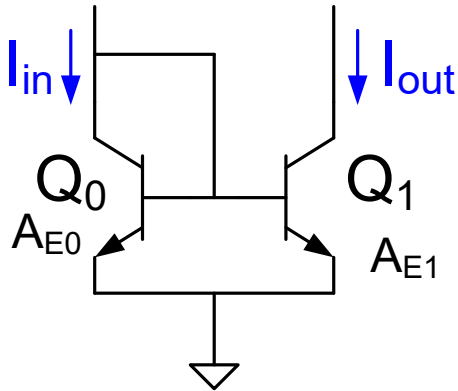


Multiple-Output Bipolar Current Source and Sink
If the base currents are neglected

$$I_{nk} = \left[\frac{A_{Enk}}{A_{E0}} \right] I_0$$

$$I_{pk} = \left[\frac{A_{En1}}{A_{E0}} \right] \left[\frac{A_{Epk}}{A_{Ep0}} \right] I_0$$

Current Sources/Mirrors



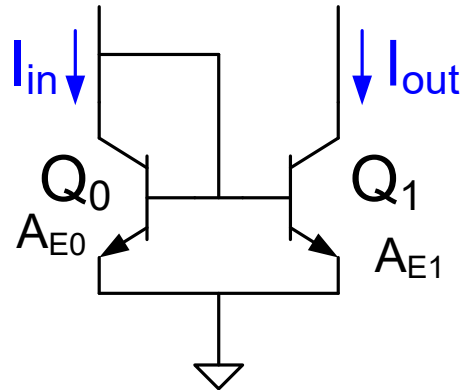
$$I_{out} = \left[\frac{A_{E1}}{A_{E0}} \right] I_{in}$$

This circuit is termed a “current mirror”

Will re-derive the transfer characteristics of the current mirror assuming I_B is small compared to I_C

$$\left. \begin{aligned} I_{IN} &= J_S A_{E0} e^{\frac{V_{BE}}{V_t}} \\ I_{OUT} &= J_S A_{E1} e^{\frac{V_{BE}}{V_t}} \end{aligned} \right\} \Rightarrow \frac{I_{OUT}}{I_{IN}} = \frac{J_S A_{E1} e^{\frac{V_{BE}}{V_t}}}{J_S A_{E0} e^{\frac{V_{BE}}{V_t}}} = \frac{A_{E1}}{A_{E0}}$$

Current Sources/Mirrors



npn Current Mirror

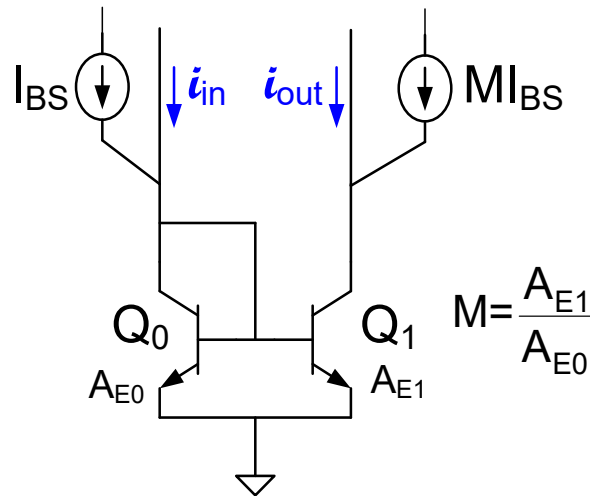
If the base currents are neglected

$$I_{out} = \left[\frac{A_{E1}}{A_{E0}} \right] I_{in}$$

- Output current linearly dependent on I_{in}
- Small-signal and large-signal relationships the same since linear
- Serves as a current amplifier
- Widely used circuit

But I_{in} must be positive !

Current Sources/Mirrors



npn current mirror amplifier

$i_{out} = ?$

$$\frac{i_{OUT} + MI_{BS}}{i_{in} + I_{BS}} = M$$

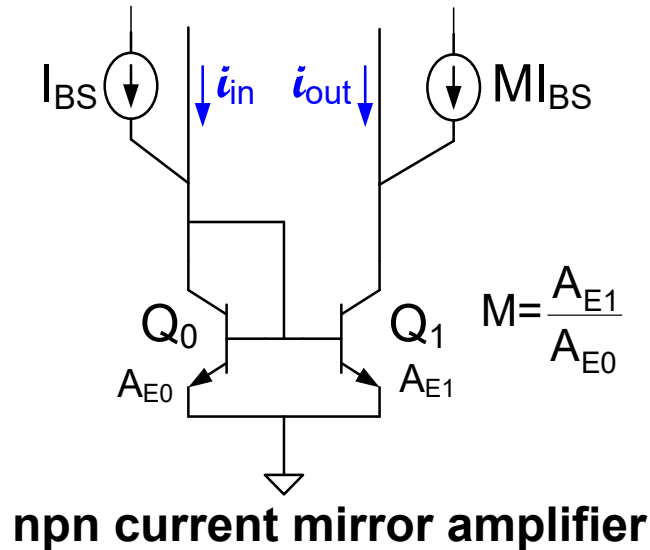
$$i_{OUT} + MI_{BS} = M(i_{in} + I_{BS})$$

$$i_{OUT} + M\cancel{I}_{BS} = M(i_{in} + \cancel{I}_{BS})$$

$$\frac{i_{OUT}}{i_{in}} = M$$

But $I_{BS} + i_{in} > 0$!

Current Sources/Mirrors



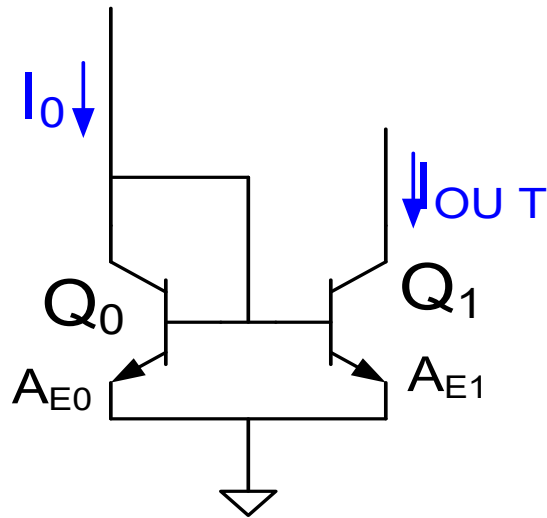
$$i_{\text{out}} = \left[\frac{A_{E1}}{A_{E0}} \right] i_{\text{in}}$$

Amplifies both positive and negative currents (provided $i_{\text{IN}} < -I_{\text{BS}}$)

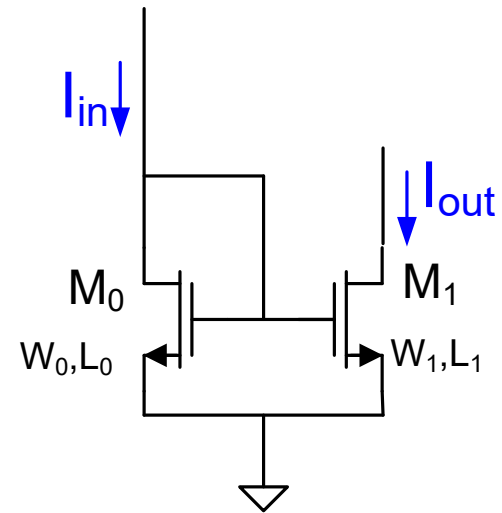
Current amplifiers are easy to build !!

Current gain can be accurately controlled with appropriate layout !!

Current Sources/Mirrors



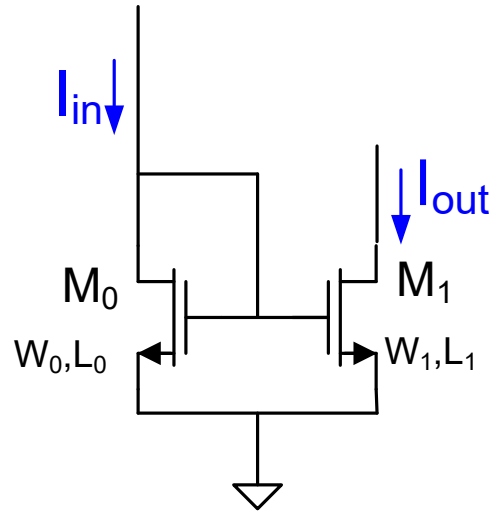
npn Current Mirror



n-channel Current Mirror

$$I_{out} = ?$$

Current Sources/Mirrors



n-channel Current Mirror

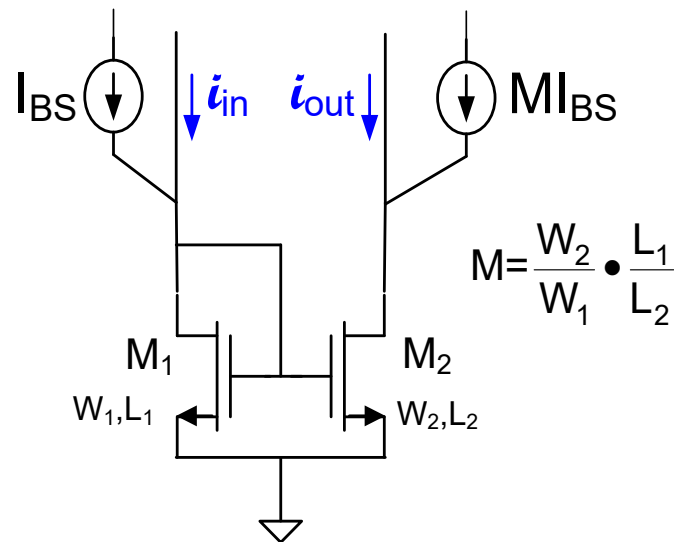
$$\left. \begin{aligned} I_{in} &= \frac{\mu C_{OX} W_0}{2L_0} (V_{GS0} - V_{T0})^2 \\ I_{out} &= \frac{\mu C_{OX} W_1}{2L_1} (V_{GS1} - V_{T1})^2 \end{aligned} \right\}$$

If process parameters are matched, it follows that

$$I_{out} = \left[\frac{W_1}{W_0} \frac{L_0}{L_1} \right] I_{in}$$

- Current mirror gain can be accurately controlled !
- Layout is important to get accurate gain (for both MOS and BJT)

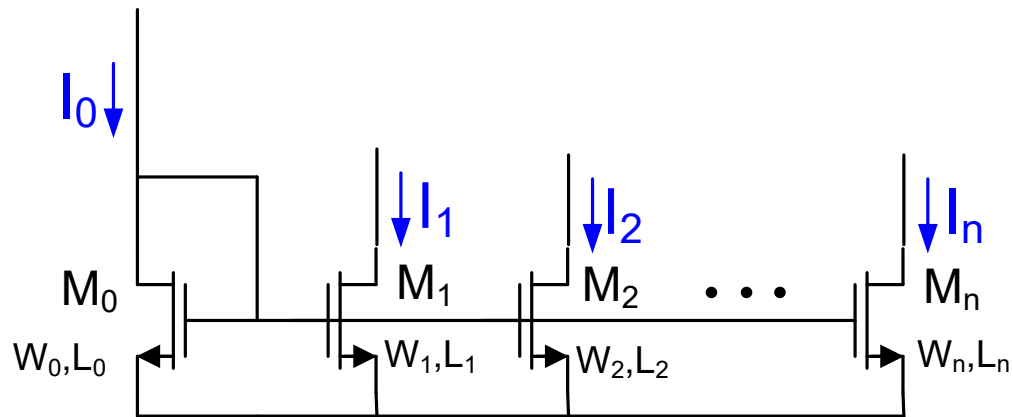
n-channel current mirror current amplifier



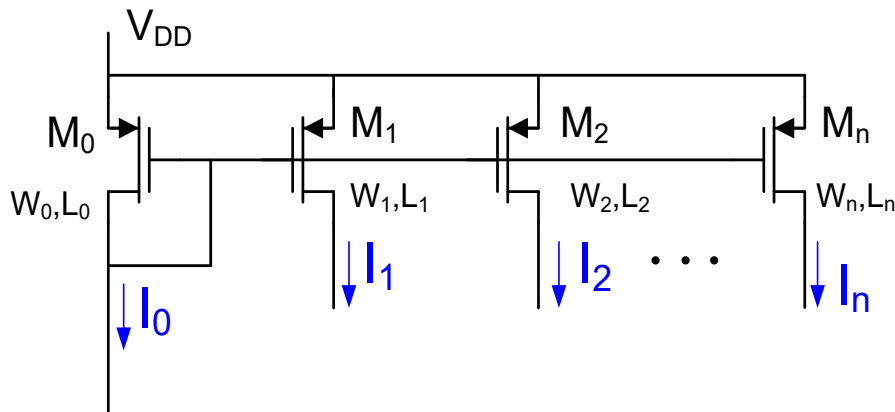
$$i_{out} = \left[\frac{W_2}{W_1} \frac{L_1}{L_2} \right] i_{in}$$

Amplifies both positive and negative currents

Current Sources/Mirrors



multiple output n-channel current sink array

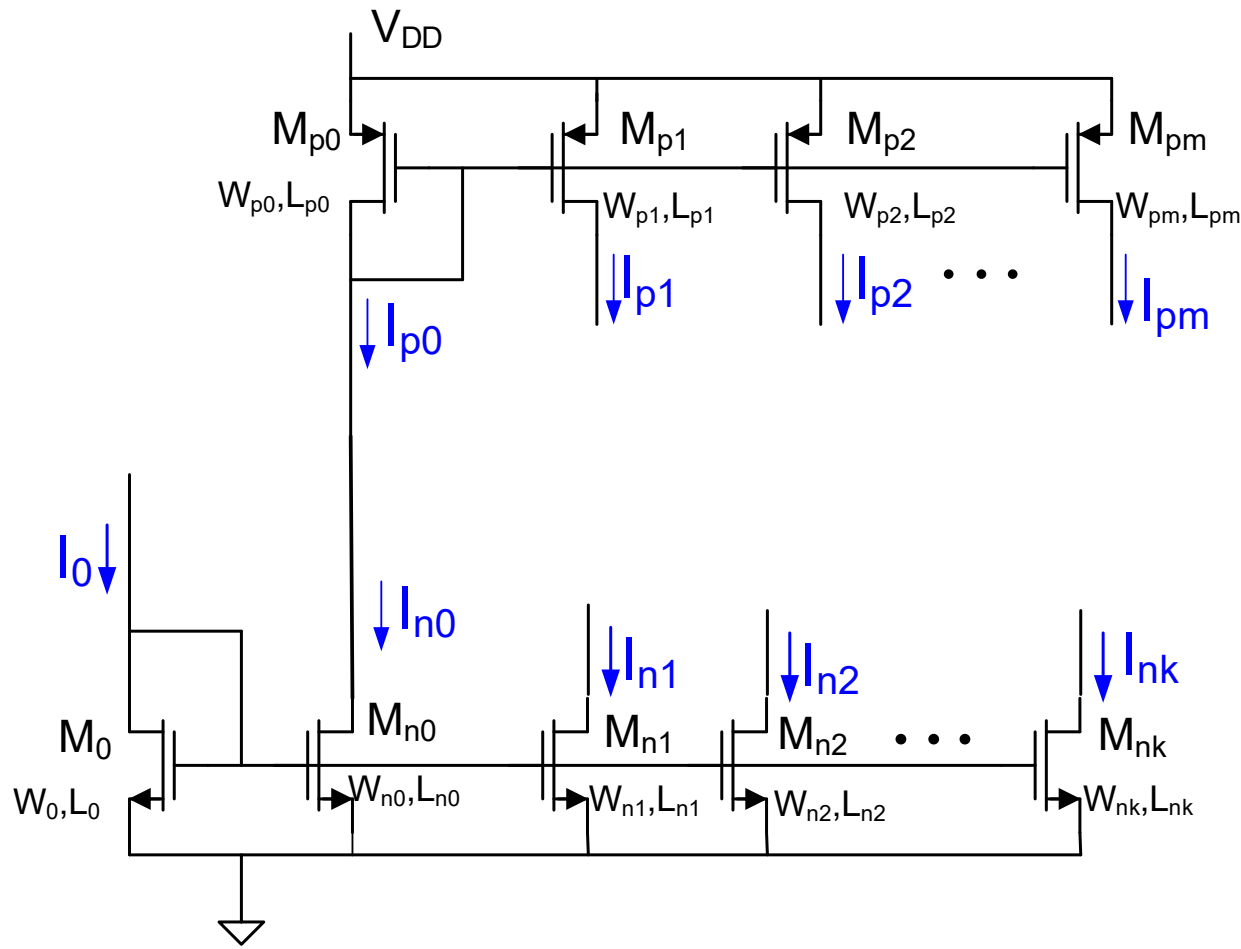


multiple output p-channel current source array

$$I_k = \left[\frac{W_k}{W_0} \frac{L_0}{L_k} \right] I_0$$

Current Sources/Mirrors

multiple sourcing and sinking current outputs



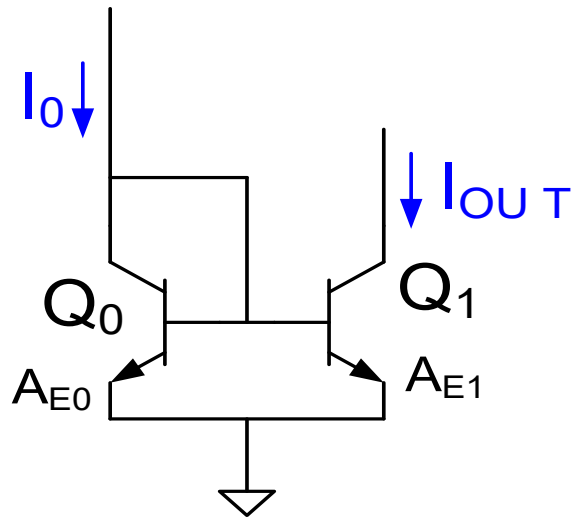
$$I_{pj} = \left[\frac{W_{pj}}{L_{pj}} \cdot \frac{L_{p0}}{W_{p0}} \right] M I_0$$

$$M = \left[\frac{W_{n0}}{L_{n0j}} \cdot \frac{L_0}{W_0} \right]$$

$$I_{nj} = \left[\frac{W_{nj}}{L_{nj}} \cdot \frac{L_0}{W_0} \right] I_0$$

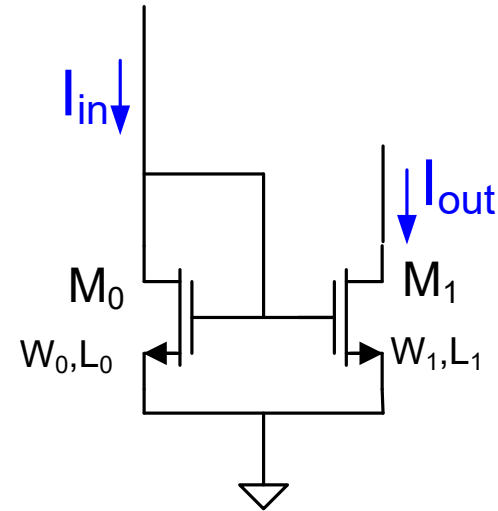
m and k may be different
Often $M=1$

Current Sources/Mirrors Summary



npn Current Mirror

$$I_{out} = \left[\frac{A_{E1}}{A_{E0}} \right] I_{in}$$



n-channel Current Mirror

$$I_{out} = \left[\frac{W_1}{W_0} \frac{L_0}{L_1} \right] I_{in}$$

- Current mirror gain can be accurately controlled !
- Layout is important to get accurate gain (for both MOS and BJT)



Stay Safe and Stay Healthy !

End of Lecture 33